

# Underestimation of the polar magnetic flux measurements due to projection effects from the ecliptic view

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## Motivation:

The distribution and evolution of the polar magnetic flux is important for solar cycle, dynamo studies and to address “solar open flux problem”.

## Polar observations are challenging from the ecliptic view:

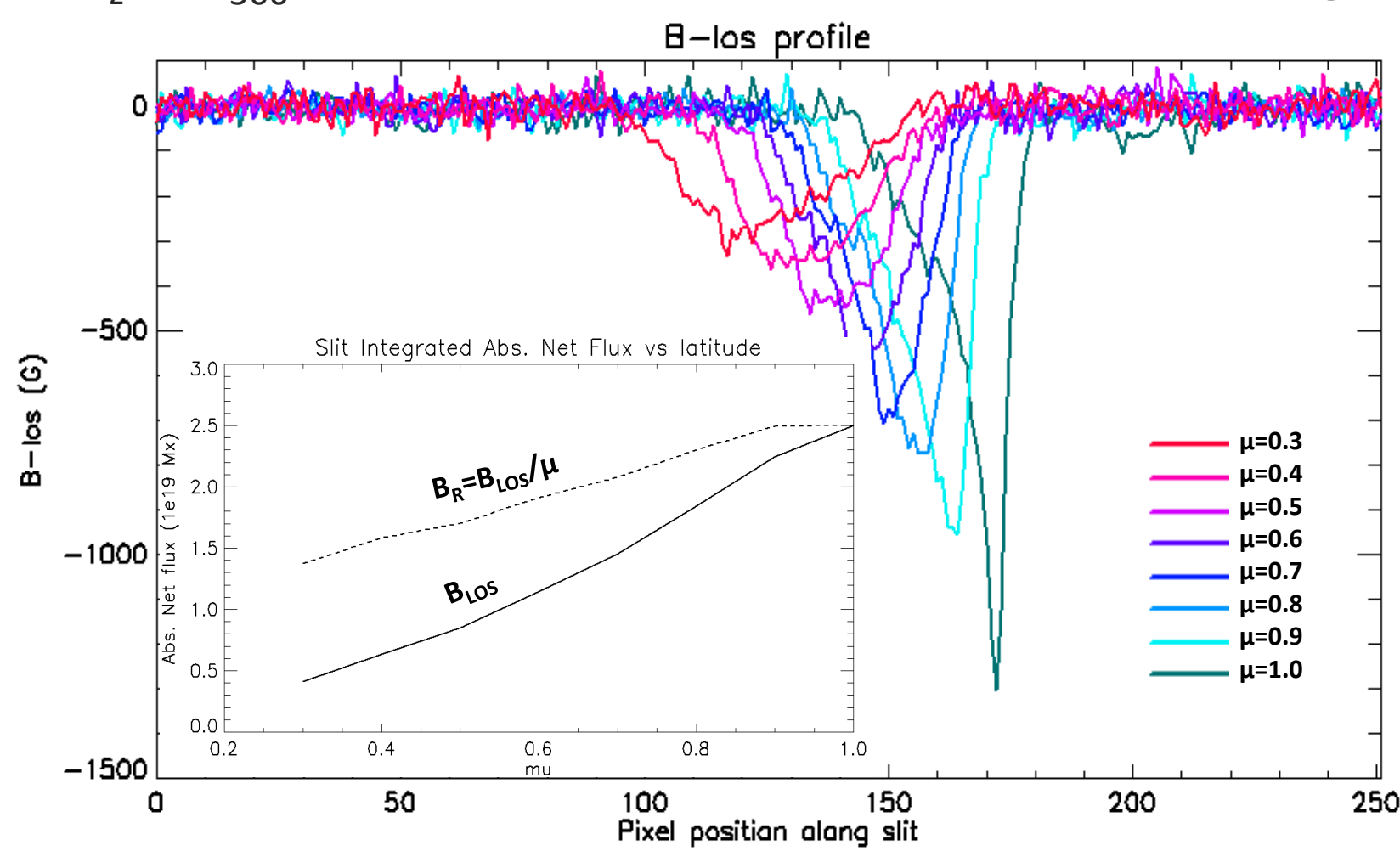
- Dominant quiet sun magnetic flux is mostly vertical:  
→ Oblique view means poor Stokes-V signals.
- Foreshortening causes coarser spatial sampling per pixel:  
→ Observed flux is underestimated due to sub-pixel flux cancellation.

## Interpretation is challenging:

- Spectral lines form over a range of heights in solar atmosphere.
- B reduces with height as flux tube expands to maintain lateral pressure balance.
- Inclined line-of-sight (LOS) samples different depth (upper layers) in solar atmosphere as compared to vertical LOS.

## Current Study:

- Considers projection effects only on LOS measurements.
- Systematic errors only: No instrumental noise considered.
- Uses realistic MHD simulations of quiet sun magnetic network as input to synthesize Stokes profiles of the Ni I 676.8 nm absorption line, of GONG and MDI heritage.
- Stokes profiles are synthesized with various ray projections ( $\mu=0.3-1.0$ ) through the model atmosphere.
- Apply center-of-gravity (COG) algorithm to the Stokes I±V profiles to infer “synthetic” LOS magnetic field ( $B_{LOS}$ ) maps.
- Use the  $B_{LOS}$  maps to study net flux variation with viewing angle.
- Actual  $B_z$  at  $\tau_{500}=1$  surface in the MHD cube is taken as the ground truth.



**Fig 3.** The profiles of  $B_{LOS}$  along the vertical dashed yellow line (“slit”) in the synthetic magnetograms shown in the mosaic of figure 1 is shown here with the profile colors coded according to the  $\mu$  value. The inset shows the variation of the absolute value of net flux ( $B_{LOS}$ ), integrated over the area covered by the slit, with  $\mu$  value. Also shown is the variation of the estimated radial flux,  $B_R = B_{LOS}/\mu$ , with  $\mu$  value (the dotted curve).

## Results:

The mean magnetic flux in solar polar regions inferred from LOS magnetographs is underestimated due to multiple reasons:

(a) The magnetic field is predominantly vertical in quiet Sun network regions → diminishing Stokes-V signal → missing weaker flux below the noise limit of the measurements.

(b) Under the assumption that field is predominantly vertical, the radial flux is estimated as  $B_R = B_{LOS}/\mu$ . This has following implications:

- Flux tubes are vertical only in the darkest intergranular lanes, flux tube expands outside this region to form a magnetic canopy.
- The canopy fields have a pseudo-bipolar appearance away from the disk center, just like unipolar round sunspots appear pseudo-bipolar when viewed away from the disk center.
- Due to foreshortening, a part of this pseudo-bipolar canopy flux would cancel due to sub-pixel cancellation.
- Even if the canopy flux is spatially resolved, applying a vertical flux assumption to pseudo-bipolar canopy flux causes artificial broadening of histogram FWHM (lower panel of Fig 2.)
- Doing spatial average (over polar regions) of the pseudo-bipolar canopy flux leads to flux cancellation and hence an underestimation of the polar flux.
- Changing B-angle of the Sun from ecliptic observations further complicates these measurements.

(c) The optical depth unity ( $\tau=1$ ) surface samples deeper parts of the flux tube atmosphere, when viewed near the disk center, as compared to inclined LOS which effectively samples progressively upper layers with viewing angle.

## Conclusions:

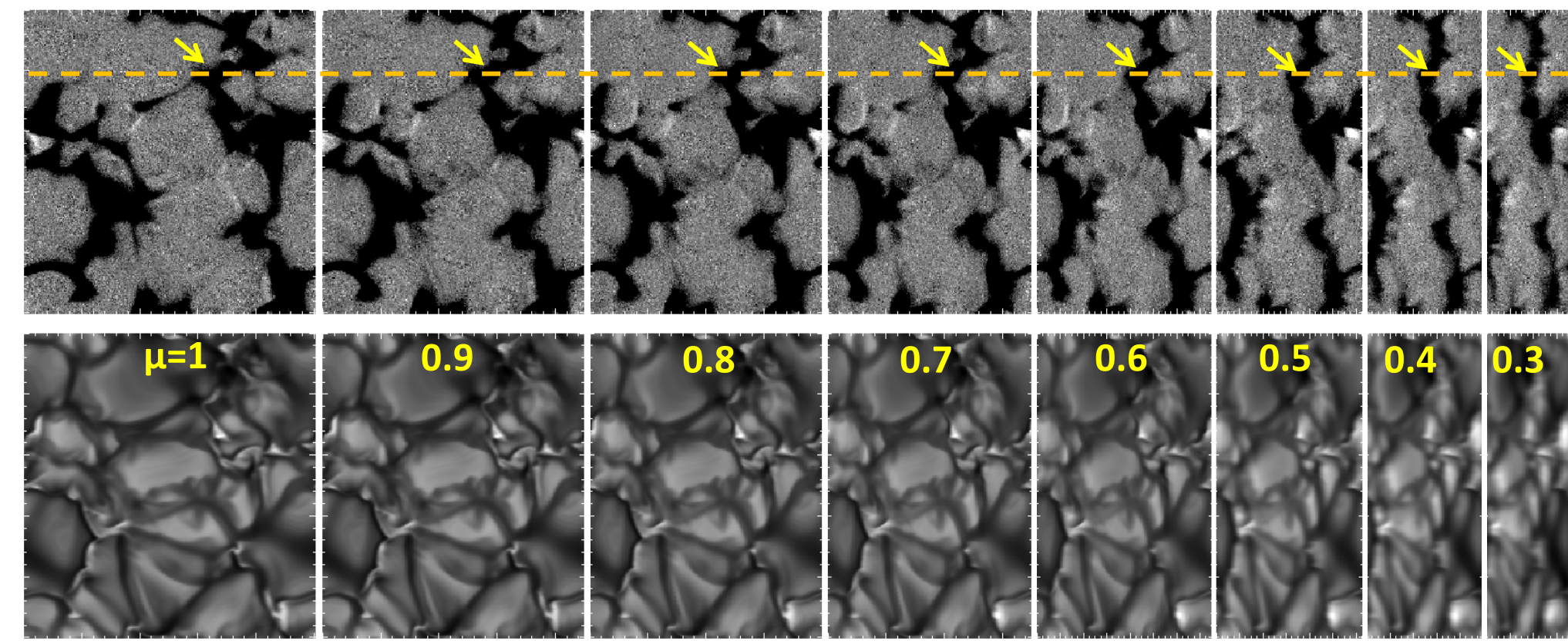
(i) LOS samples progressively upper layers of the flux tube atmosphere where the magnetic configuration is no longer dominantly vertical but more of a canopy-like configuration.

(ii) The deep-rooted stronger vertical flux remains obscured/poorly viewed from the inclined LOS. Unfortunately, the approximation  $B_R = B_{LOS}/\mu$  is only valid for this vertical part of the flux tube.

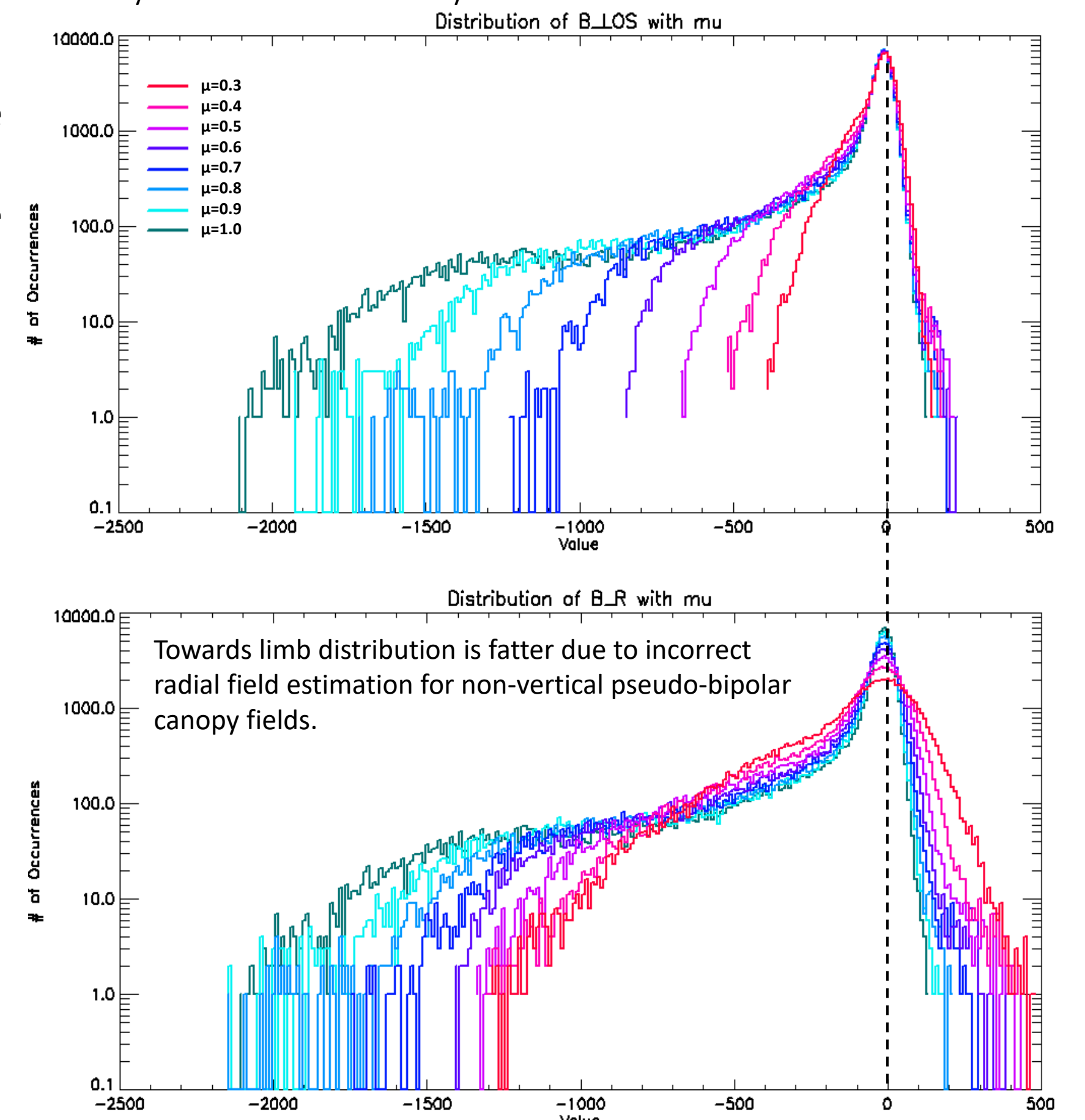
(iii) The inclined view samples the canopy region of flux tube giving a pseudo-bipolar appearance which does not contribute to net flux estimates when simply spatially averaged and/or due to foreshortening caused sub-pixel cancellation.

(iv) In principle vector field measurements should help, however, they suffer from issues such as magnetic fill factor, 180-degree azimuth ambiguity and differential QU versus V noise issues.

(v) Out of ecliptic observations, such as from polar flyby orbit proposed for Solaris mission, would help to resolve the true polar magnetic flux.



**Fig 1.** A mosaic of synthetic LOS magnetograms (left column) and the continuum intensity map (right column) computed for different viewing angles ( $\mu = \cos \theta$ ) from a numerical MHD and radiative transfer model of the quiet Sun network is shown. Geometric foreshortening along y-direction and “bread loaf” like appearance of granules can be noticed. The yellow arrow shows the network lane feature which is sampled along vertical dashed yellow line for further study.



**Fig 2.** The histograms of the  $B_{LOS}$  as inferred from various viewing angles ( $\mu = \cos \theta$ ) is shown in top panel where  $\mu$  is color coded. The number of pixels measuring stronger flux reduces systematically as is expected for the case of predominantly vertical flux tubes in intergranular network region. Traditionally, the radial flux  $B_R (= B_{LOS}/\mu)$  is computed from  $B_{LOS}$  under the assumption that flux is predominantly vertical outside of the active regions. The histograms of the  $B_R$  flux inferred under this assumption at various  $\mu$  is shown in the bottom panel.

