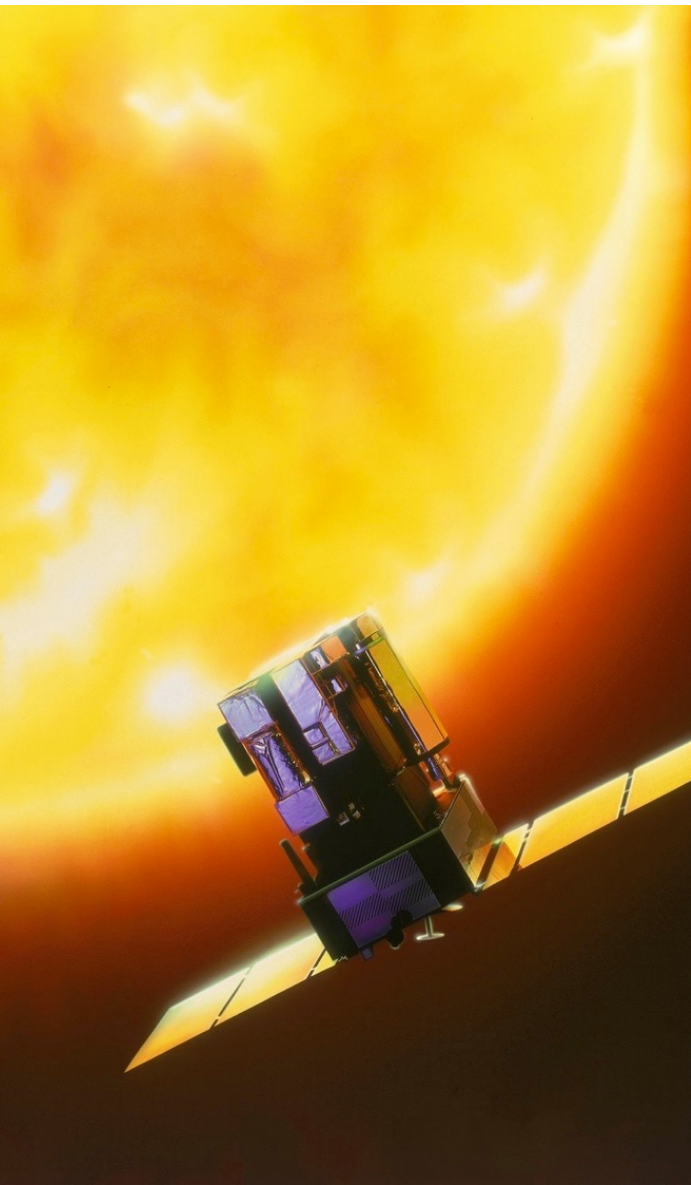


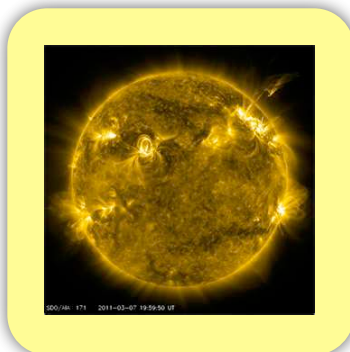
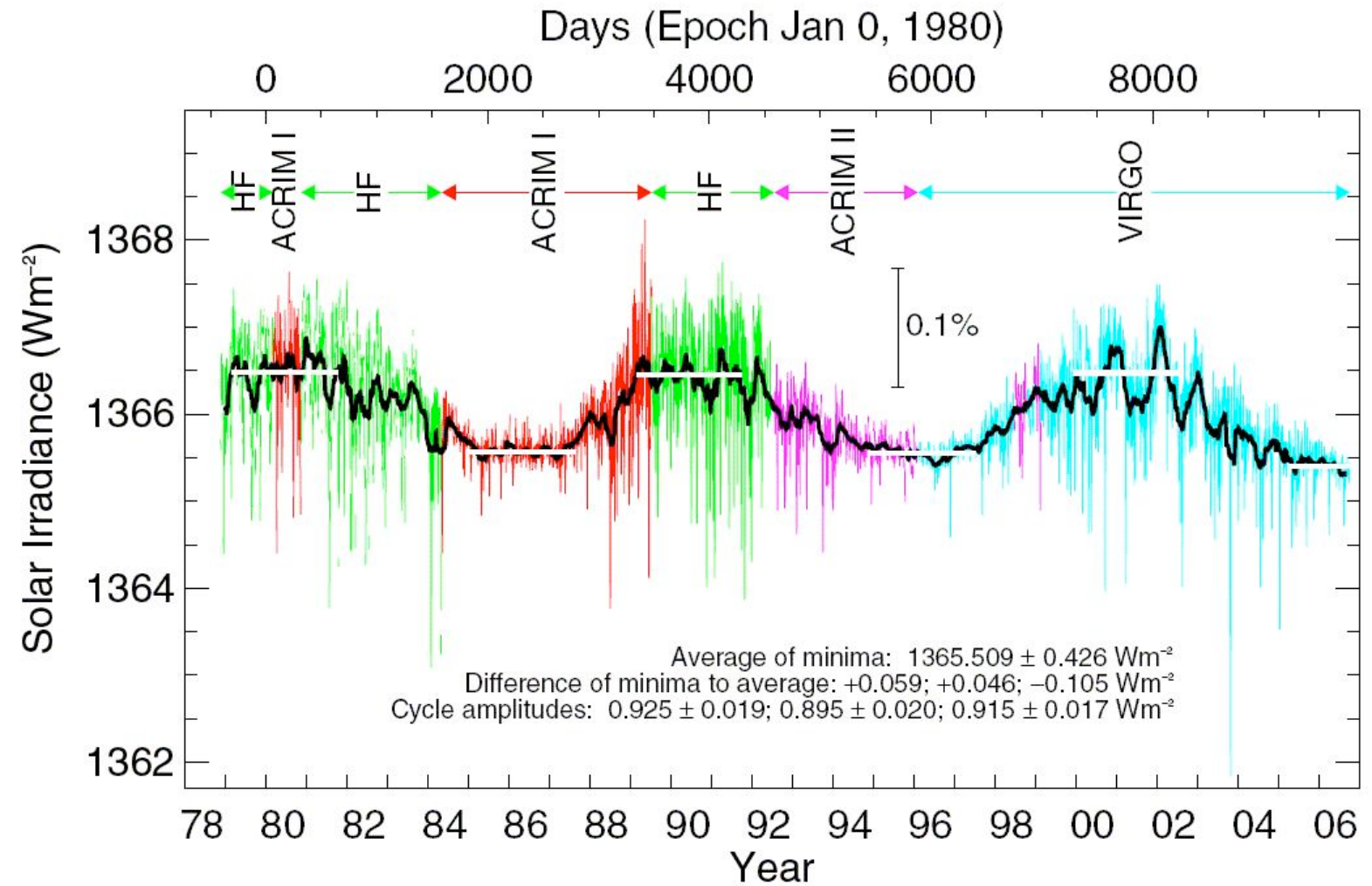
THOMAS KALLINGER

**ANOTHER OBSERVERS
POINT OF VIEW ON
STELLAR GRANULATION**

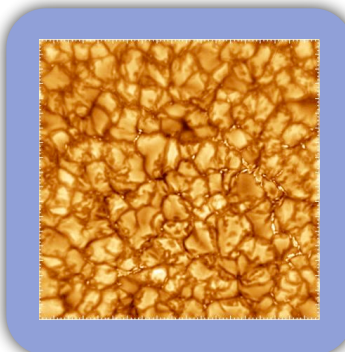
THE SOLAR SIGNAL



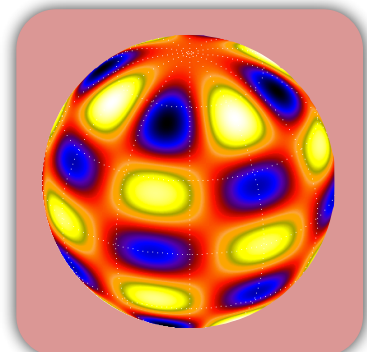
SOHO/VIRGO



activity



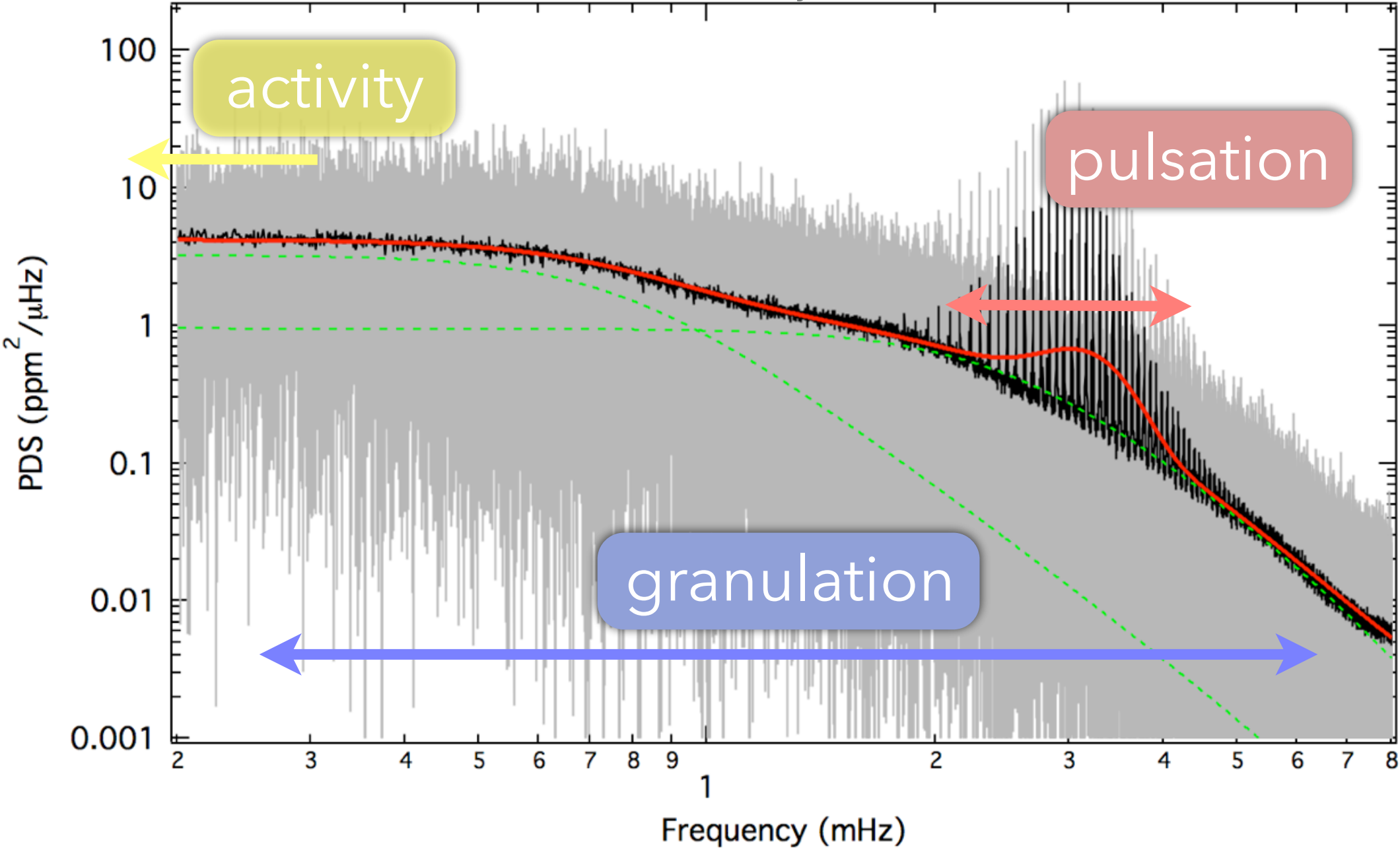
granulation



pulsation

THE SOLAR SIGNAL

1 year of VIRGO data at solar minimum



GLOBAL MODEL

noise granulation pulsation

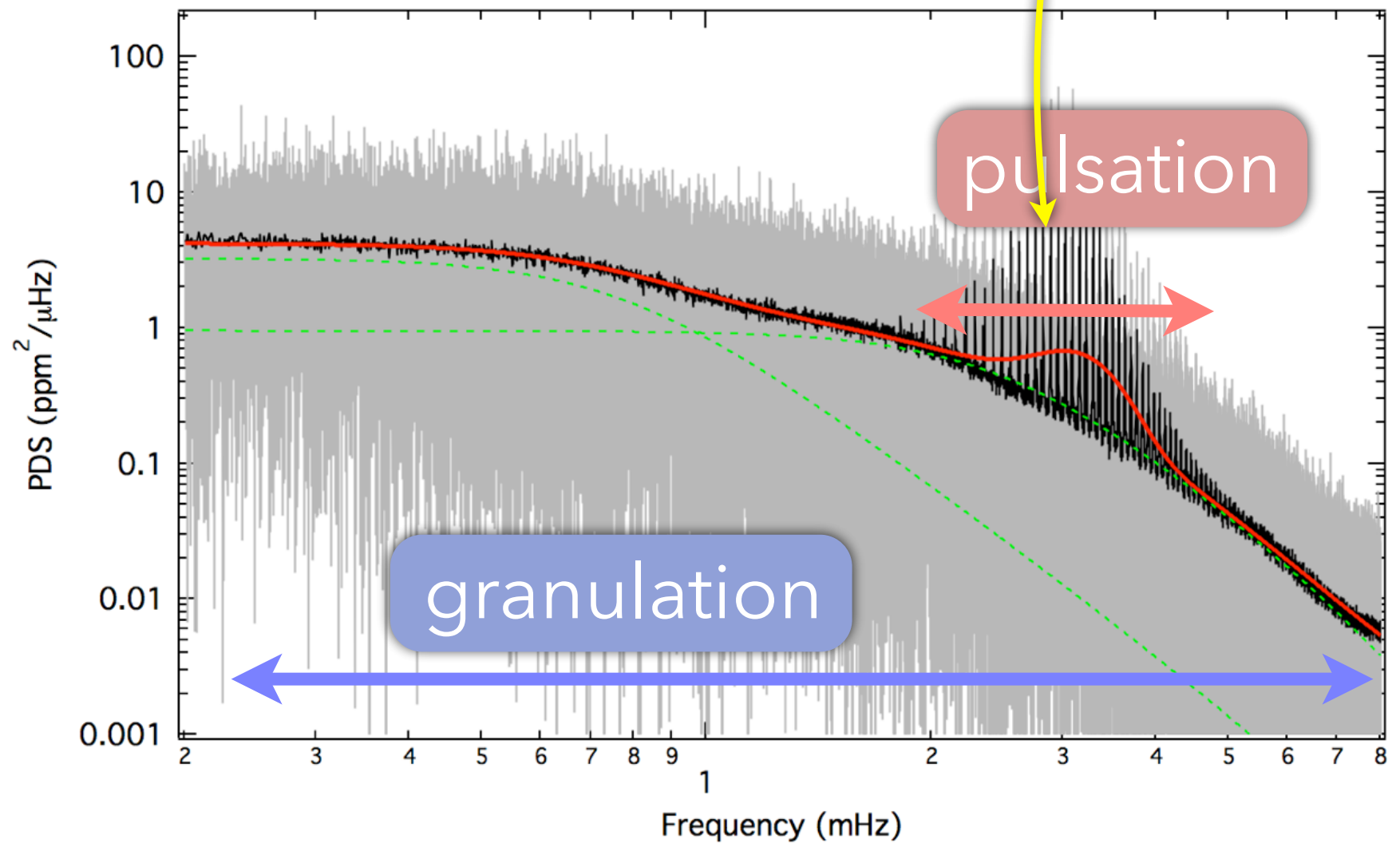
$$P(\nu) = P_n + \sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^4} + P_g \exp \frac{-(\nu_{max} - \nu)^2}{2\sigma_g^2}$$

“granulation” parameters

τ ... time scale

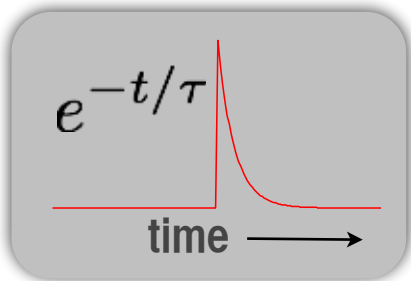
σ ... amplitude

ζ ... normalisation constant

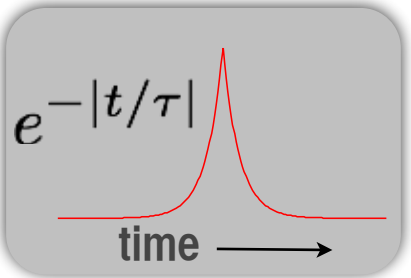


HARVEY'S MODEL ZOO

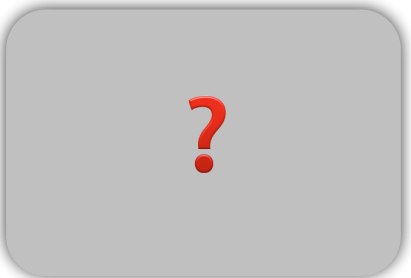
e.g.



$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^2}$$



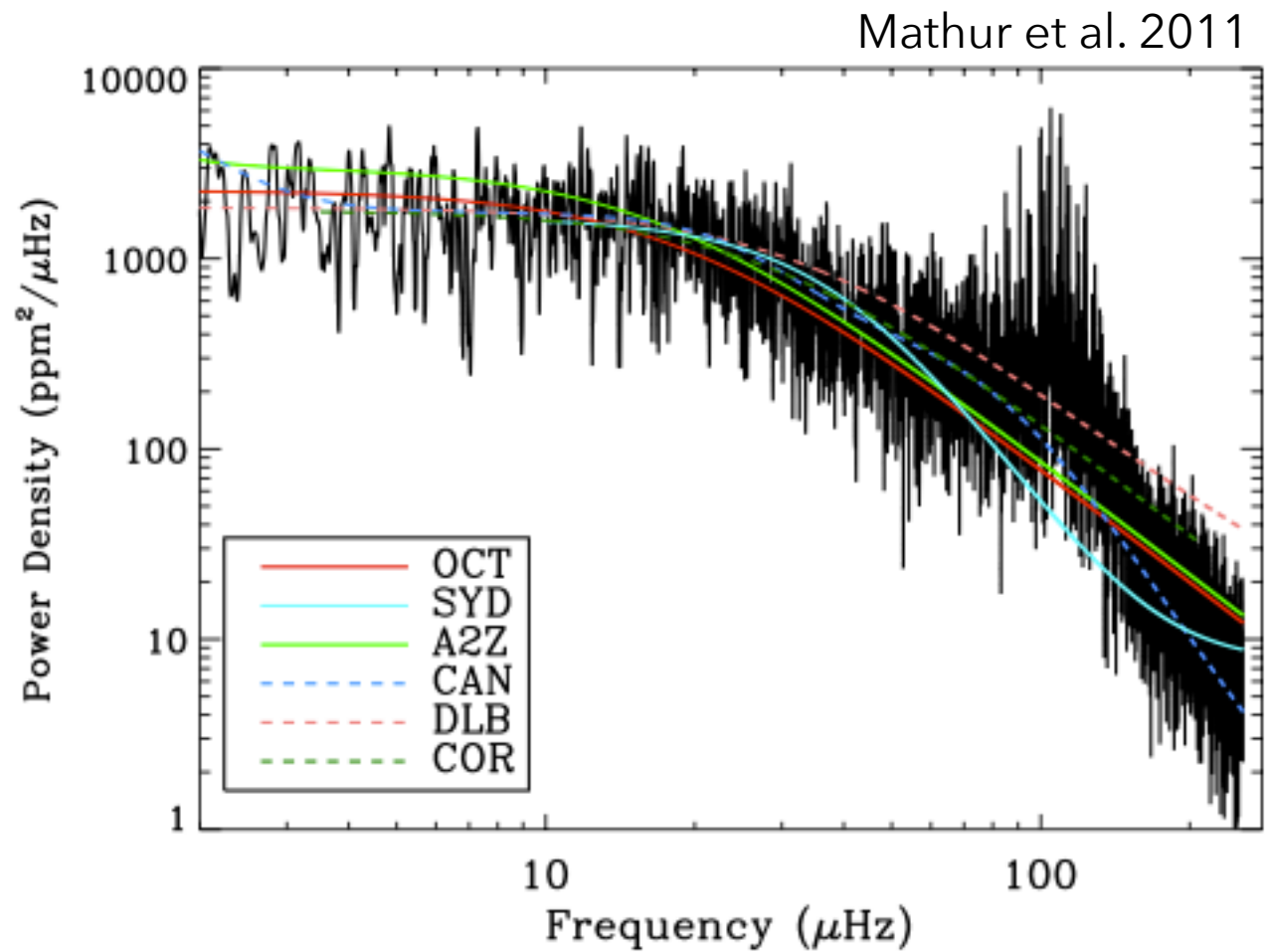
$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{[1 + (2\pi\nu\tau_i)^2]^2}$$



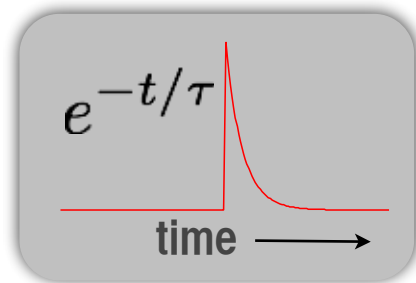
$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^4}$$



$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^{\alpha_i}}$$



HARVEY'S MODEL ZOO

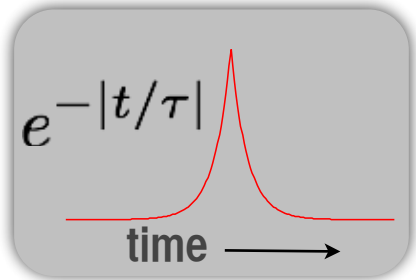


e.g.

$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^2}$$



$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^4}$$



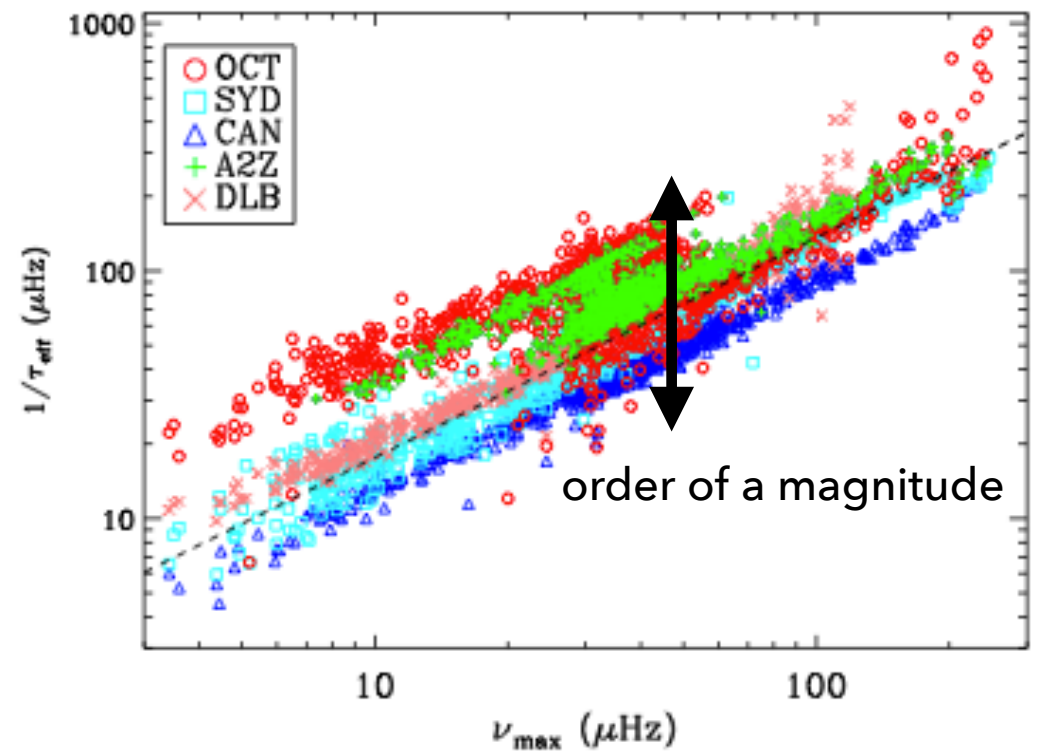
$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{[1 + (2\pi\nu\tau_i)^2]^2}$$



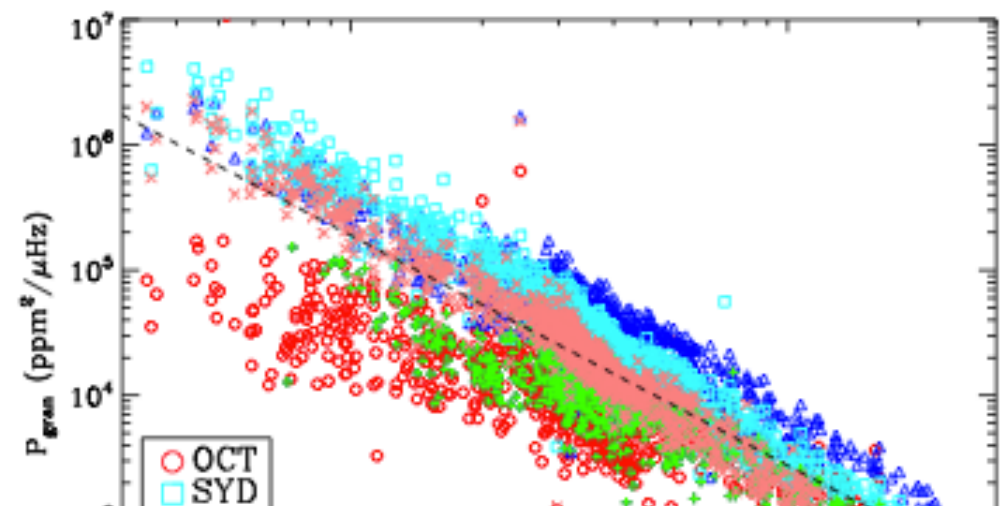
$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^{\alpha_i}}$$

Mathur et al. 2009

timescales



"amplitudes"



Bayesian model comparison

ν_{max} (μHz)

PICKING THE RIGHT MODEL

the tool ...

MultiNest

Feroz et al. 2009

... Bayesian Nested Sampling Algorithm

- probability distributions for the parameters
- global evidence for the fit

A/E

$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^2}$$

B/F

$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^4}$$

C/G

$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{[1 + (2\pi\nu\tau_i)^2]^2}$$

D/H

$$\sum_i \frac{\zeta \sigma_i^2 \tau_i}{1 + (2\pi\nu\tau_i)^{\alpha_i}}$$

$i=1,2$... 1 or 2 components

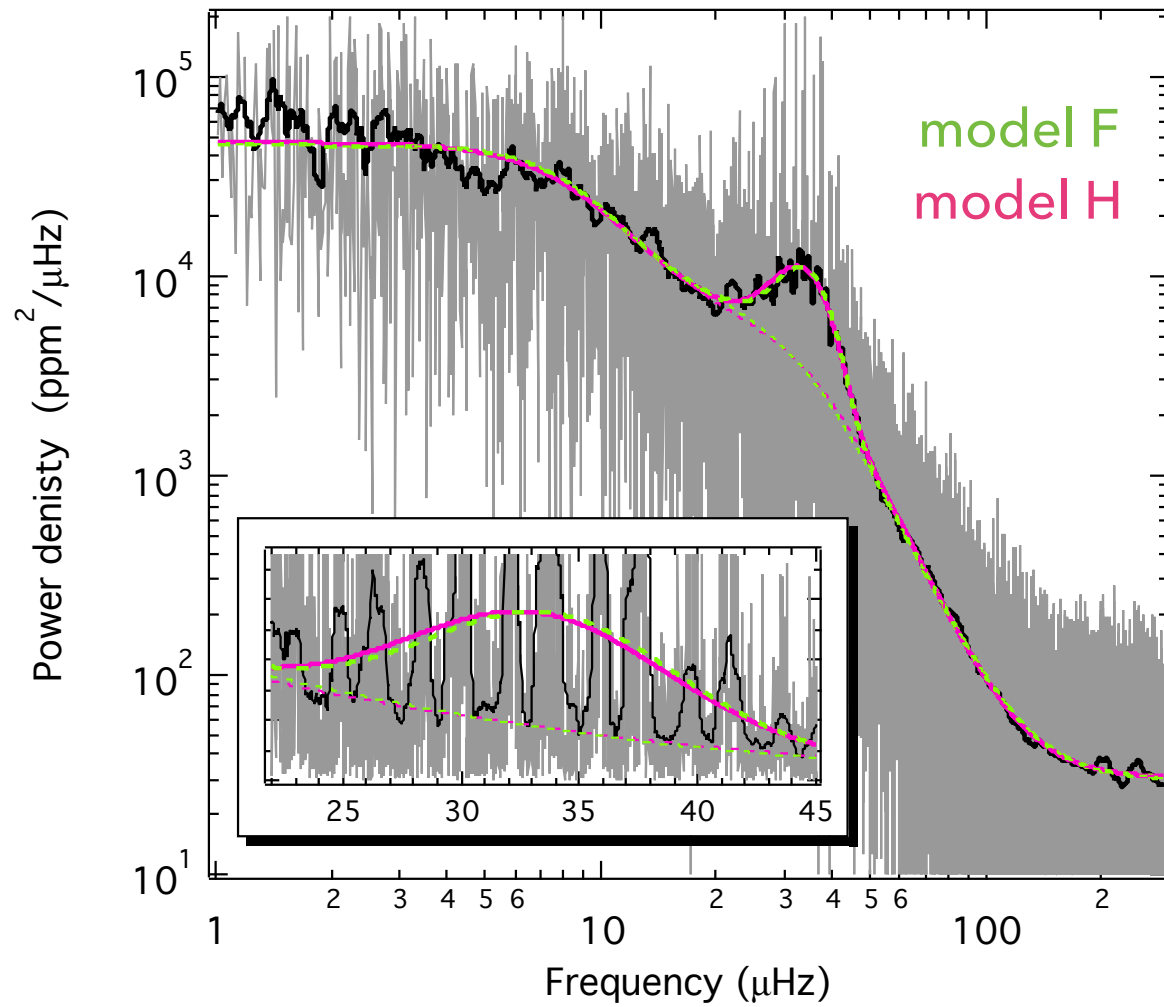
	$\ln(z/z_0)$	p	P_g	Gaussian ν_{\max}	σ	1 st component			2 nd component		
						a_1	b_1	c_1	a_2	b_2	c_2
A	-1587.7	$< 10^{-200}$	5.4(2)	30.38(02)	13.1(2)	560(12)	2.3(1)	2*			
B	-255.7	$\sim 10^{-111}$	4.8(3)	35.7(3)	5.1(2)	624(6)	23.7(2)	4*			
C	-75.8	$\sim 10^{-33}$	5.5(3)	34.5(2)	6.0(1)	606(6)	22.5(2)	2/4*			
D	-243.4	$\sim 10^{-102}$	5.1(3)	35.2(2)	5.7(2)	601(28)	20.8(4)	3.7(1)			
E	-1592.4	$< 10^{-200}$	5.4(2)	30.42(02)	13.2(2)	571(15)	2.3(2)	2*	31(4)	34.1(6)	2*
F	-1.7	0.166	5.5(2)	33.8(4)	6.1(2)	466(14)	9.4(5)	4*	399(19)	31.9(1)	4*
G	-36.6	$\sim 10^{-16}$	5.7(2)	33.9(2)	6.4(2)	352(26)	8.5(9)	2/4*	502(18)	25.7(6)	2/4*
H	-0.1	0.833	5.6(3)	33.5(5)	6.1(3)	470(35)	9.7(6)	3.6(3)	365(59)	35.8(3)	4.2(2)

Kallinger et al. (2014)

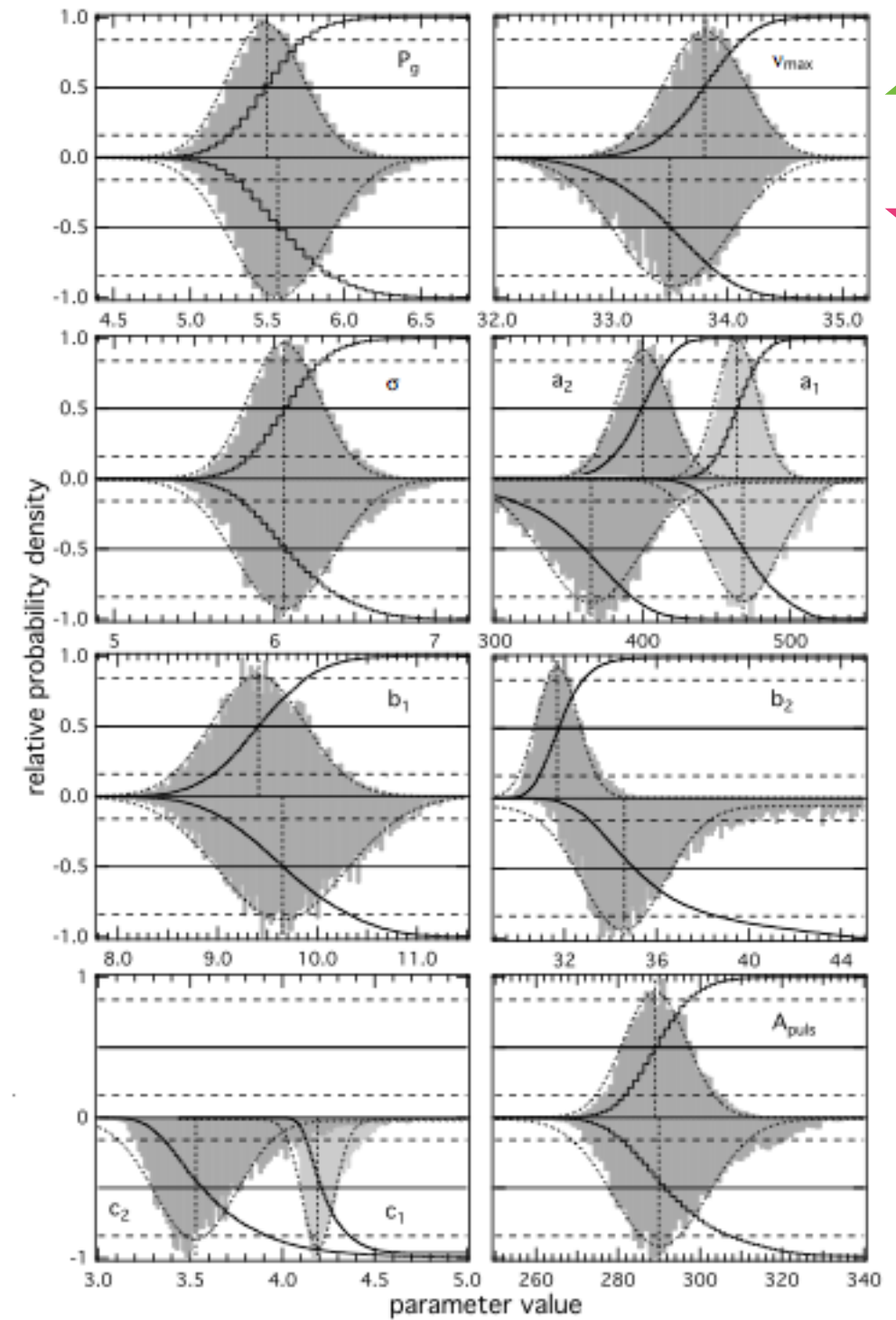
the winner is...

2 component model F and H

THE WINNING MODEL(S)

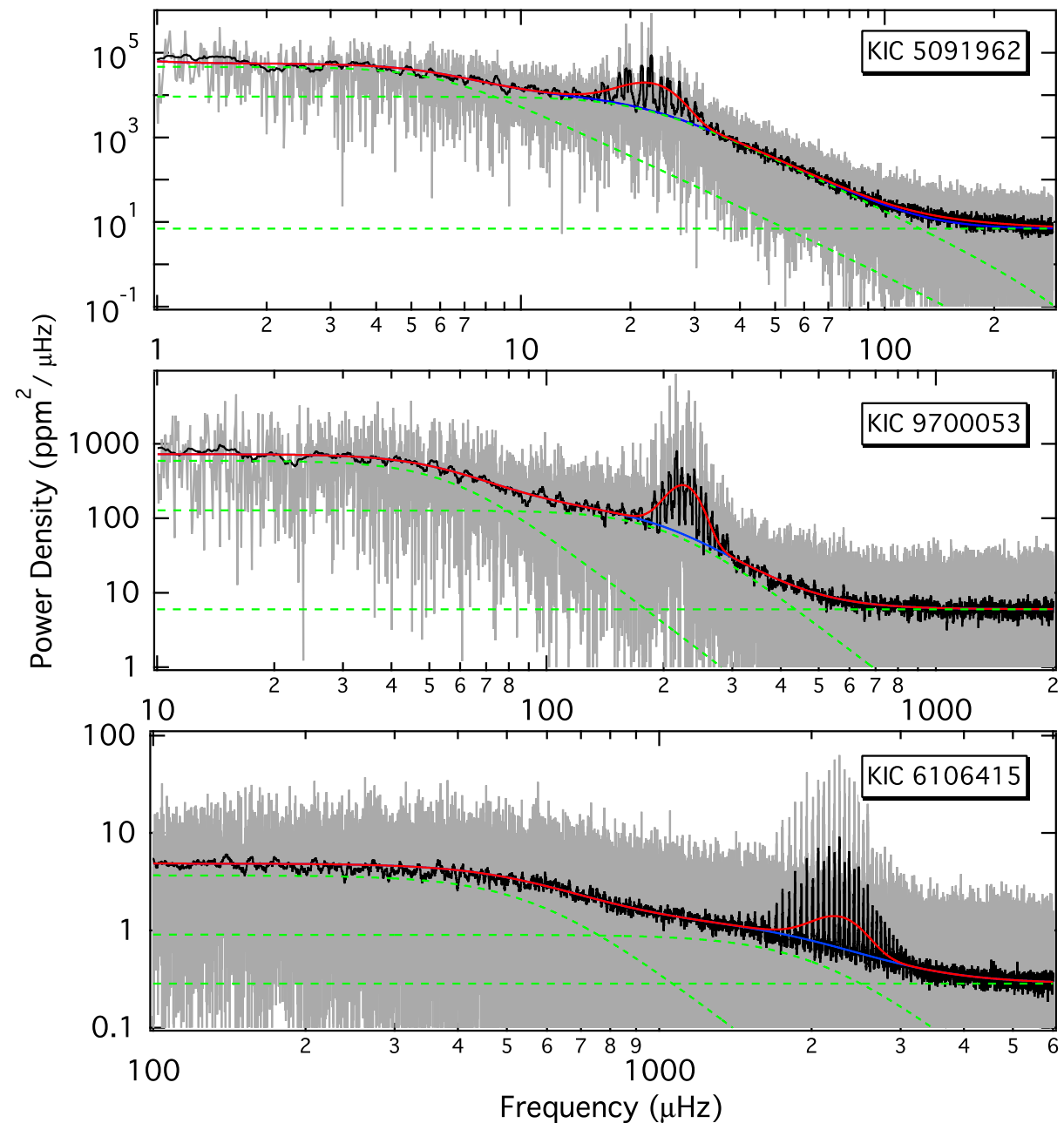


posterior distributions



Bayesian analysis tells us...

- the original Harvey model is obsolete
- reliably fitting α is difficult (even with the long Kepler time series)
- a simple super-Lorentzian works for **ALL** stars and gives reliable parameters



UNIFORM SCALING

granulation parameters
almost perfectly scale with
pulsation frequencies

timescales/frequencies

$$\text{high-freq. component: } \nu \sim 0.98 v_{\max}^{0.99}$$

$$\text{low-freq. component: } \nu \sim 0.32 v_{\max}^{0.97}$$

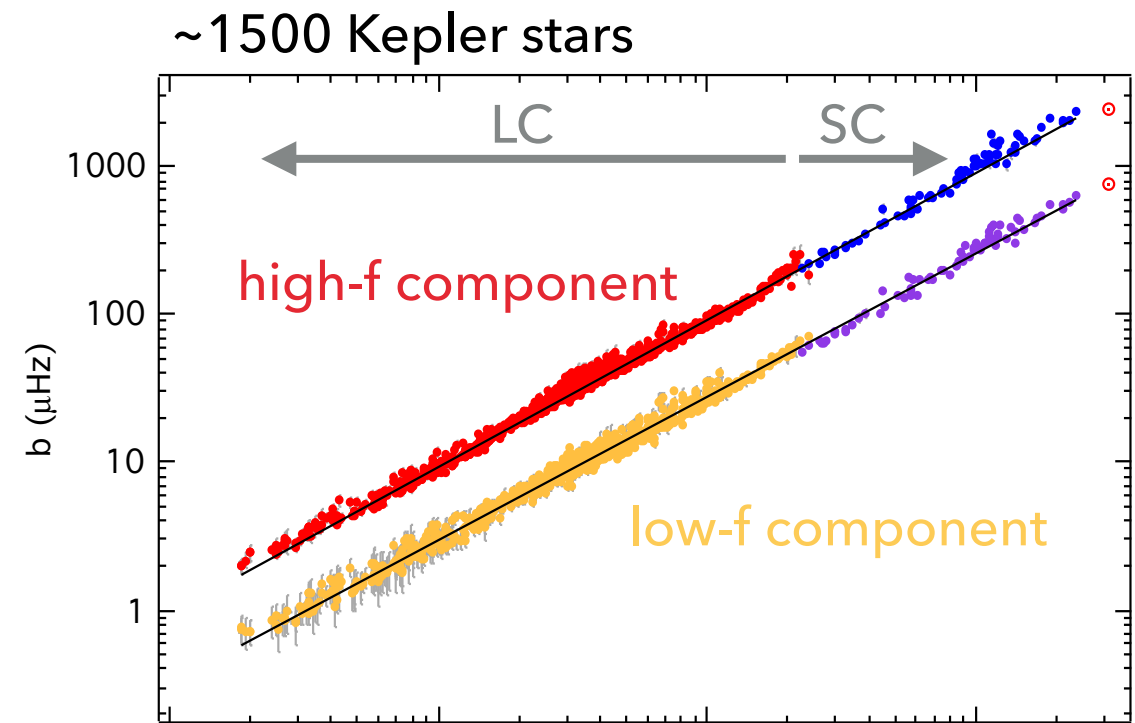
$$\nu_{\text{high}}/\nu_{\text{low}} \sim 3.06$$

$$\text{combined timescale: } \tau \sim g^{-0.85} T_{\text{eff}}^{-0.4}$$

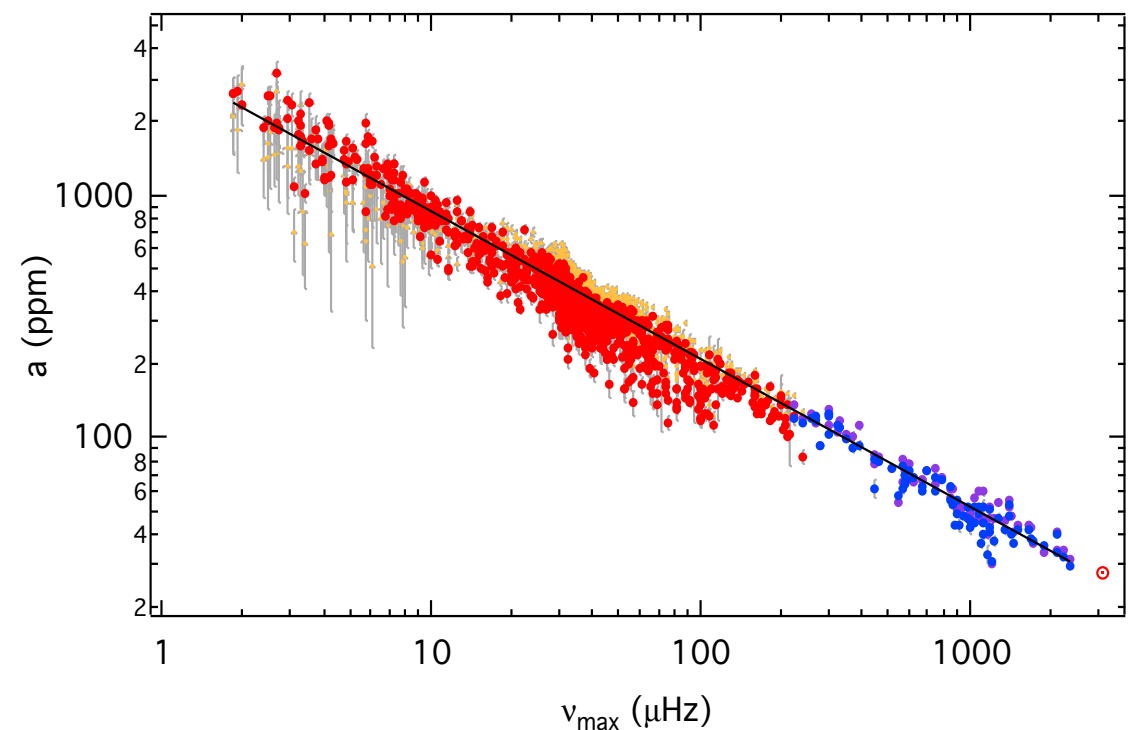
amplitudes

$$a \sim v_{\max}^{0.6}$$

$$a \sim v_{\max}^{0.6} M^{-0.25}$$



pulsation frequency



ENERGY PARTITION

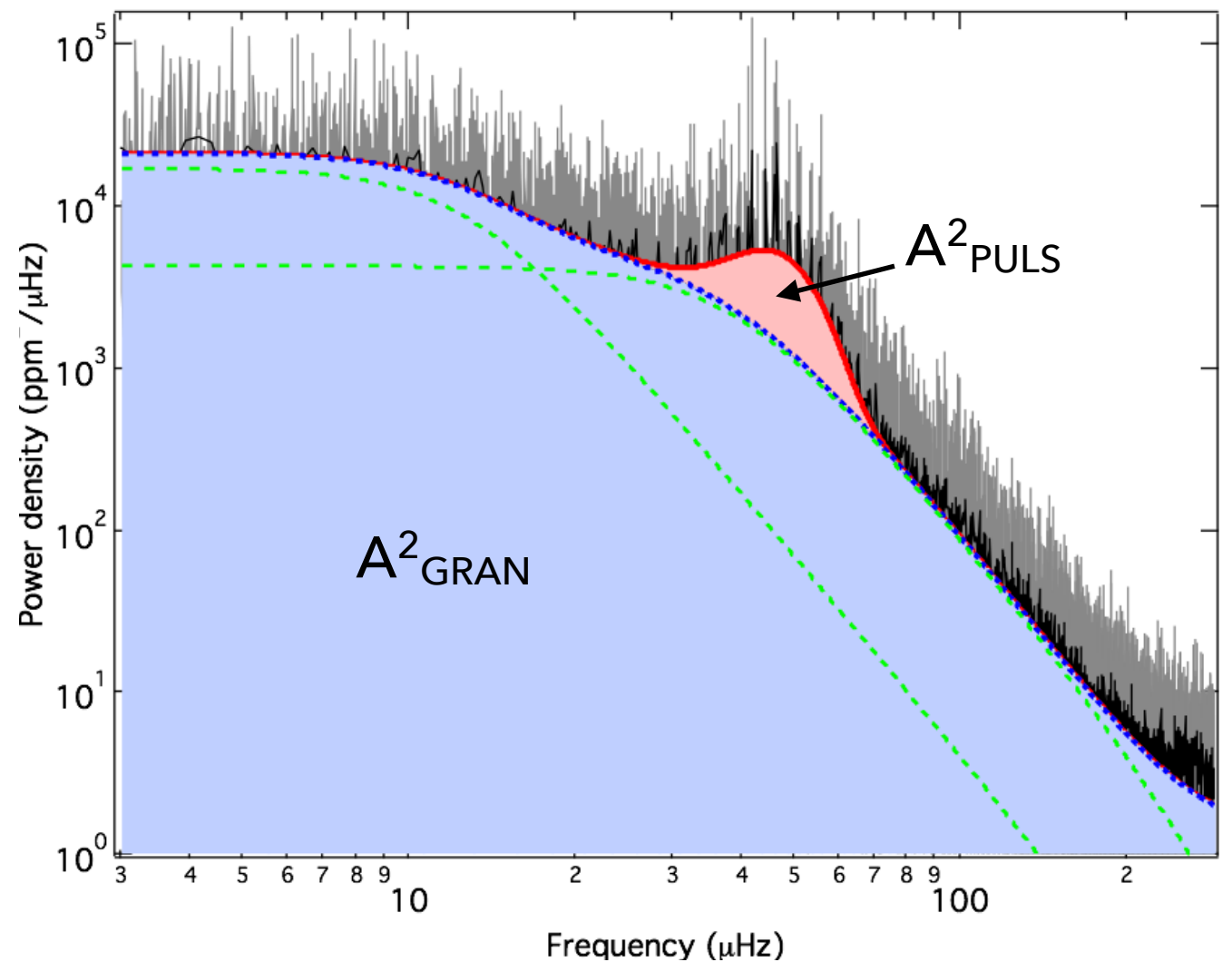
∫ spectrum ⇔ variance of the time series

pulsation energy (A^2_{PULS})

$$A^2_{\text{PULS}} = \int \text{Gaussian} = \sqrt{2\pi} P_g \sigma$$

granulation energy (A^2_{GRAN})

$$A^2_{\text{GRAN}} = \sigma_1^2 + \sigma_2^2$$



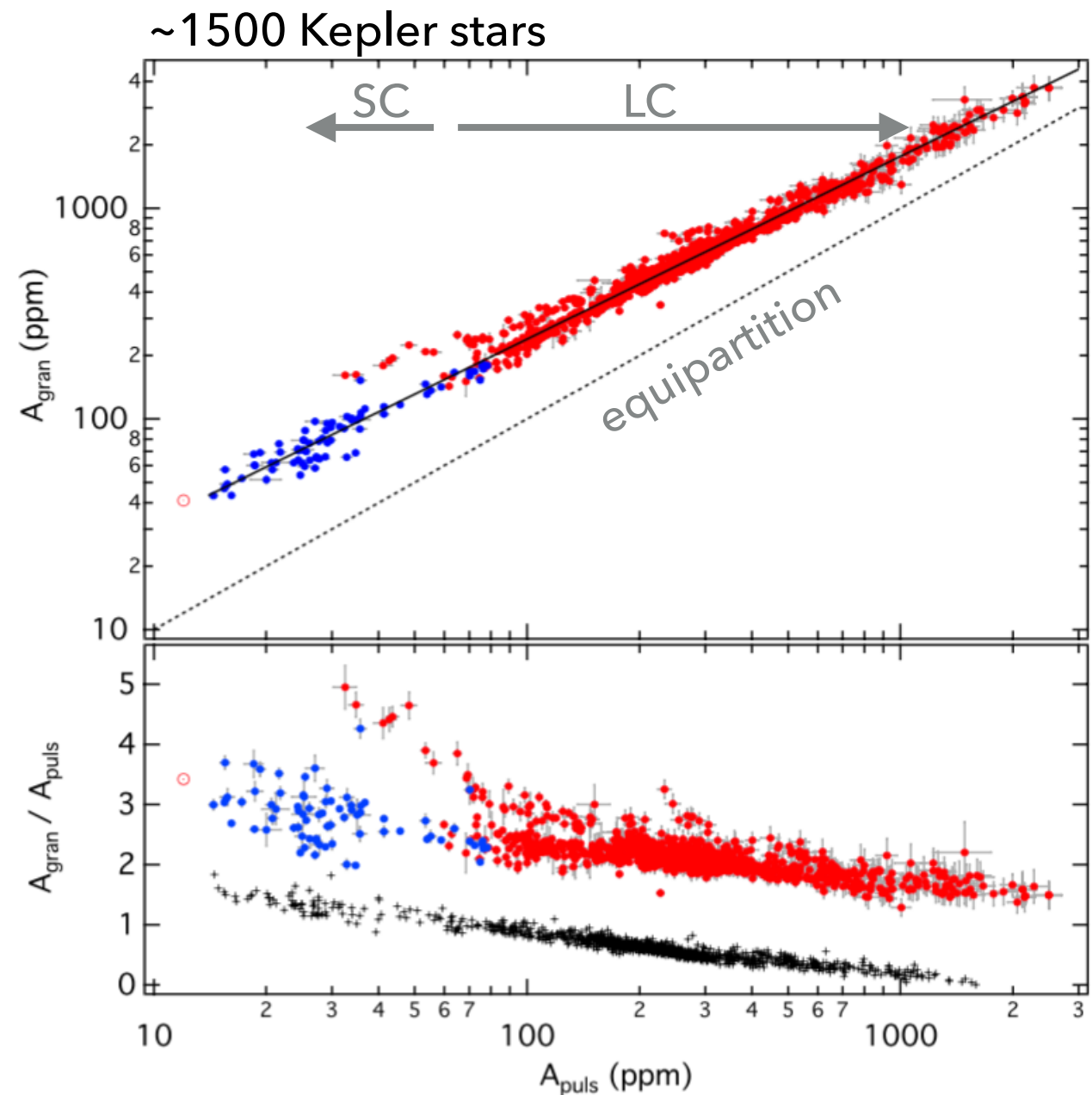
ENERGY PARTITION

$$A_{\text{GRAN}} \sim A_{\text{PULS}}^{0.86}$$

dependence on surface gravity (g) and mass (M)

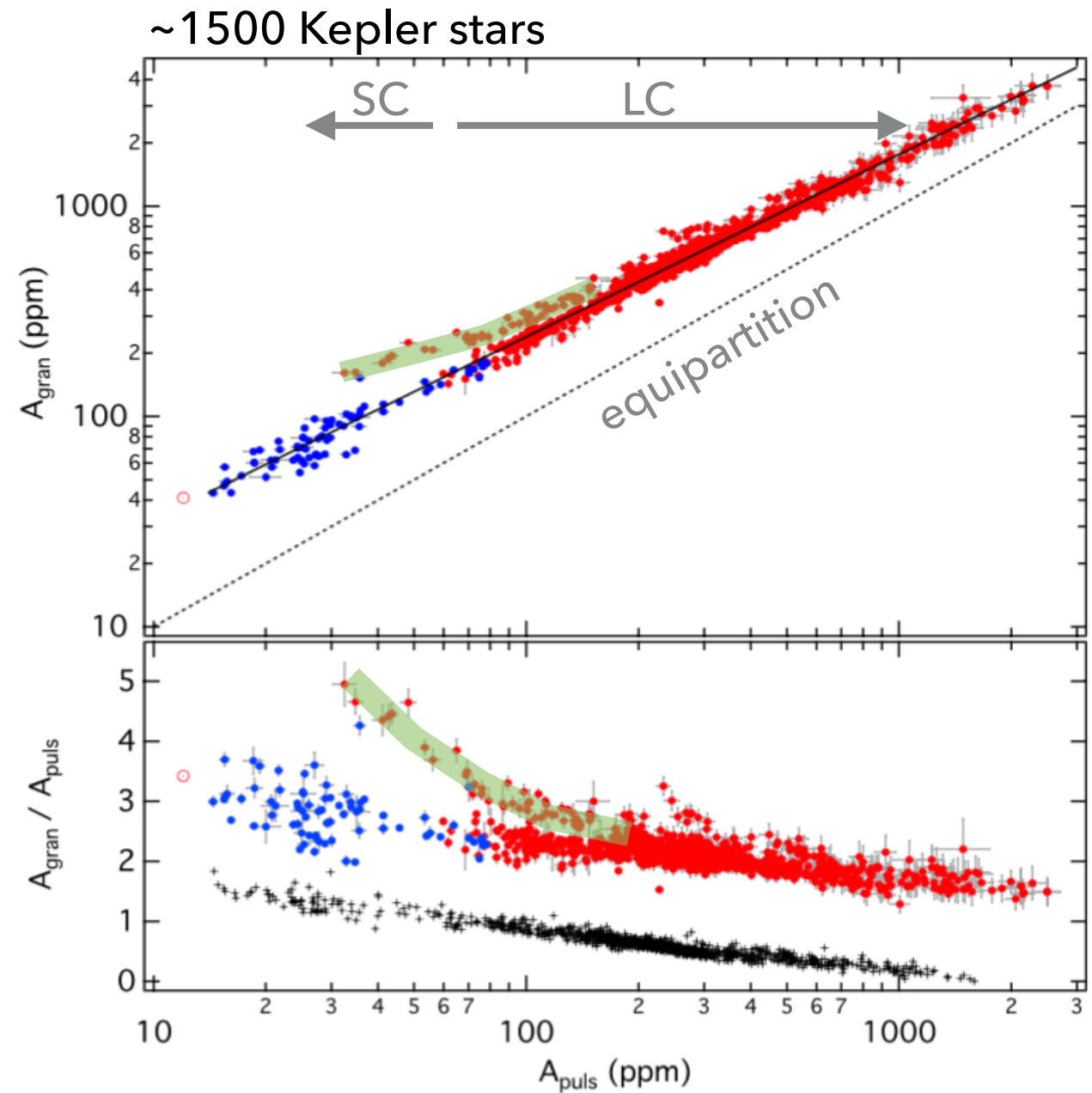
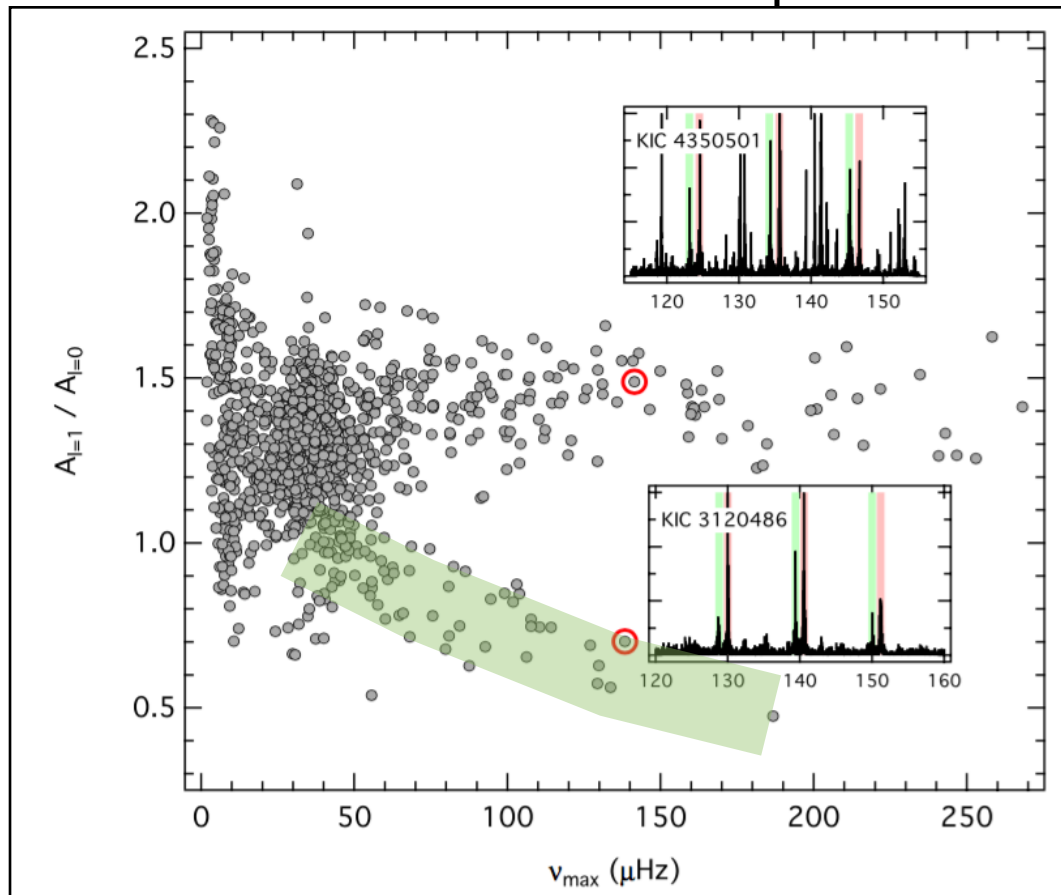
$$A_{\text{GRAN}} \approx g^{-1/2} M^{-1/4}$$

$$A_{\text{PULS}} \approx g^{-2/3} M^{-1/3}$$



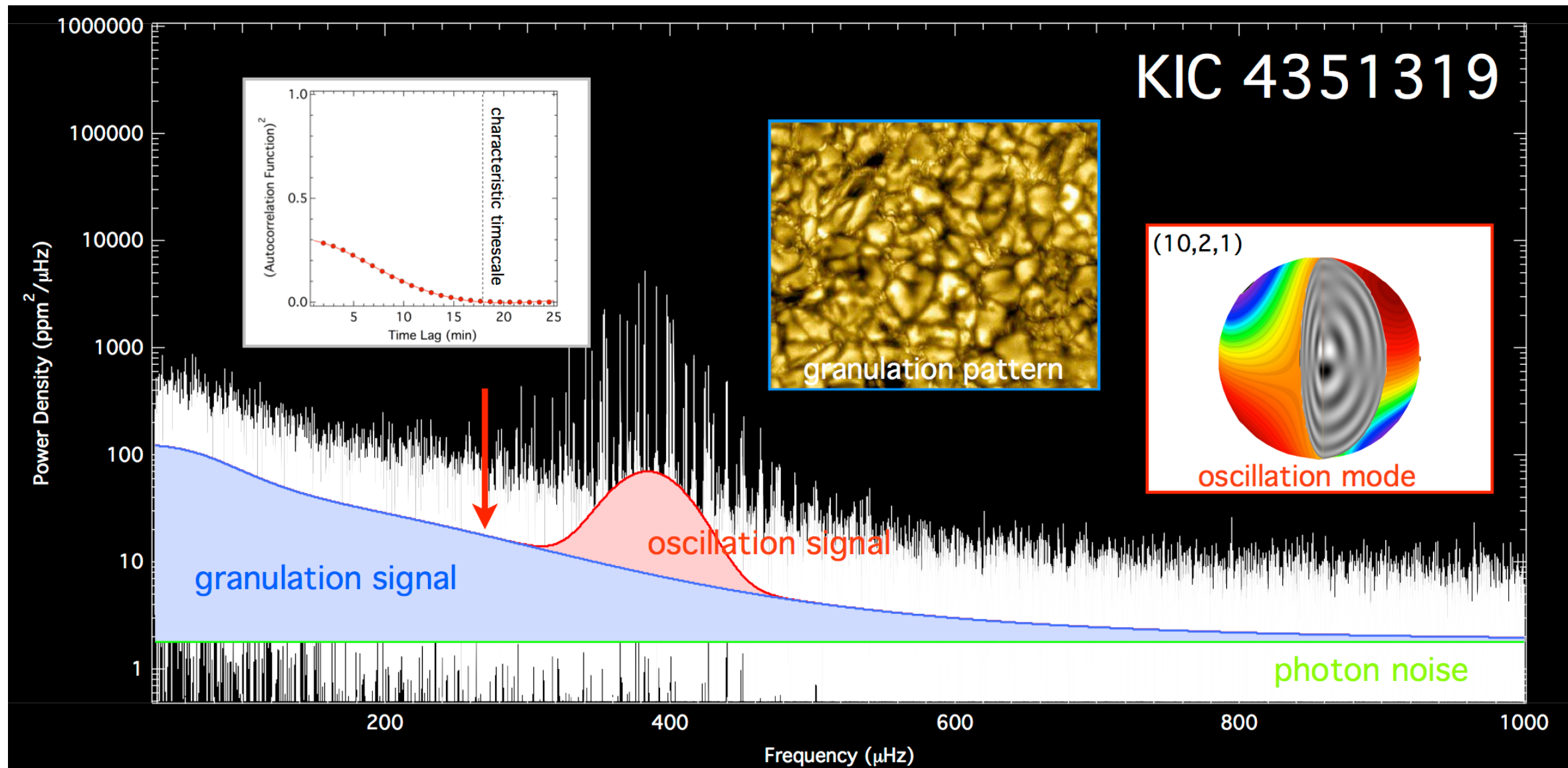
DEPRESSED DIPOLE MODES

$l=1/l=0$ amplitude ratio



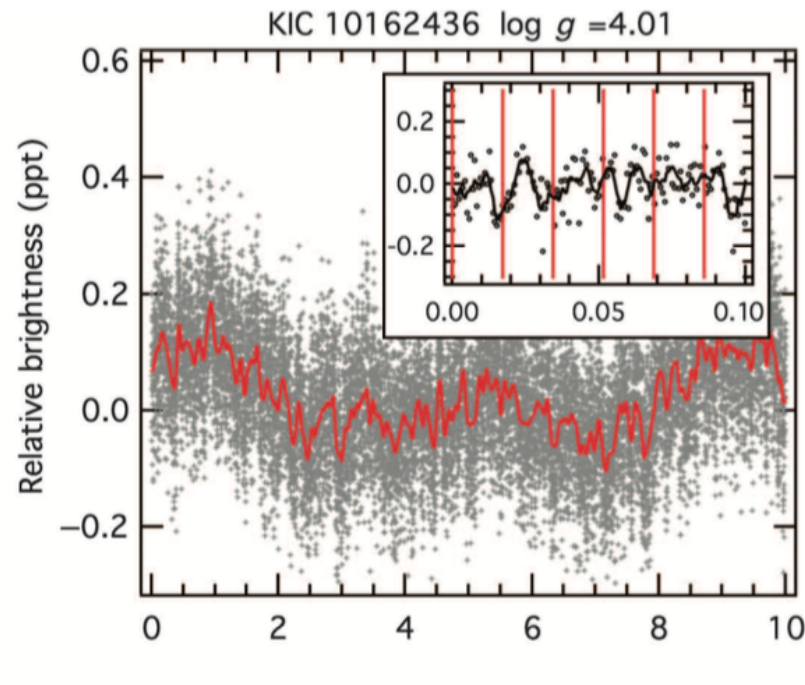
IMPLICATIONS FOR FUNDAMENTAL PARAMETER ESTIMATES

A NEW WAY TO MEASURE SURFACE GRAVITY

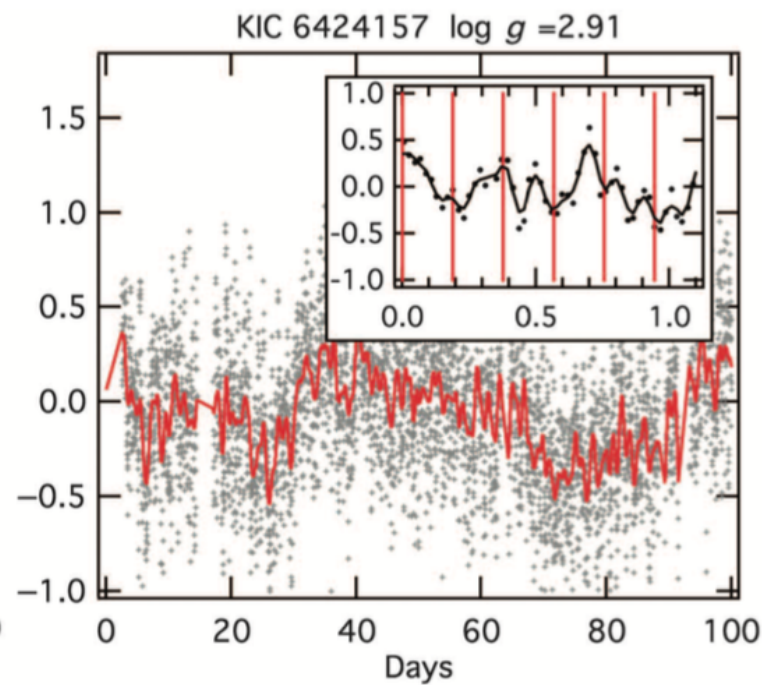


AUTOCORRELATION TIMESCALE

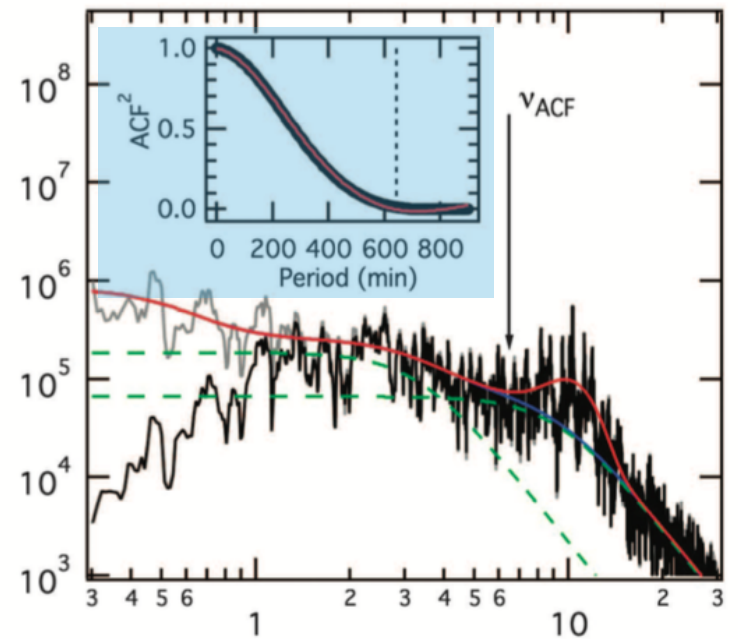
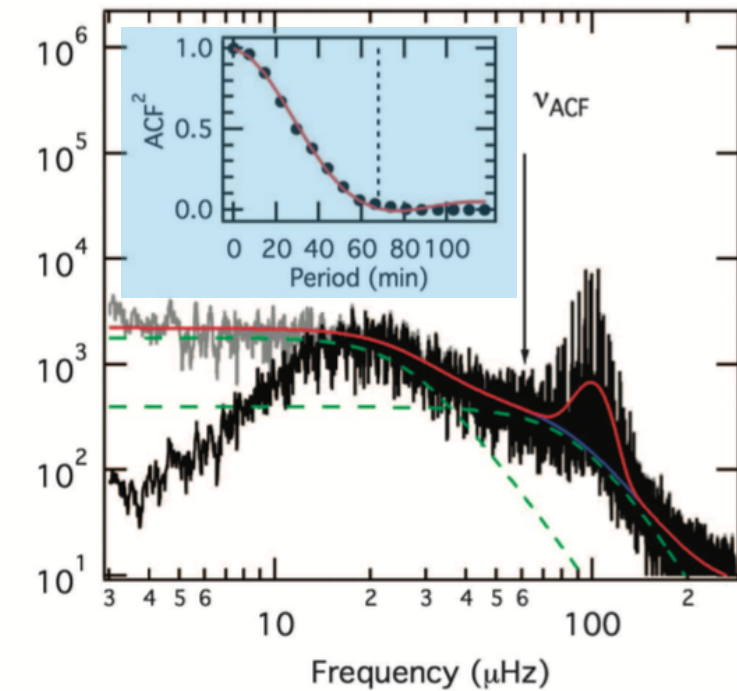
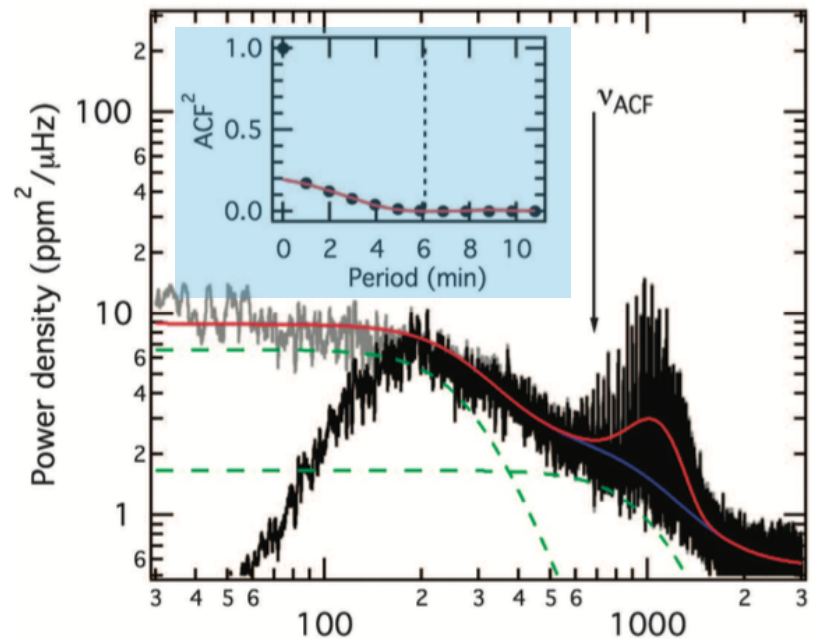
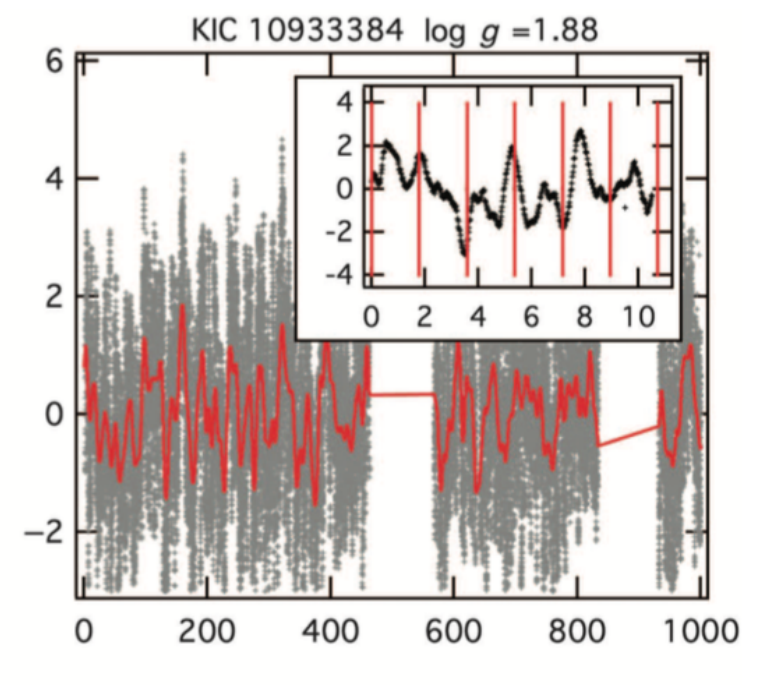
main sequence



low-luminosity RGB



high-luminosity RGB

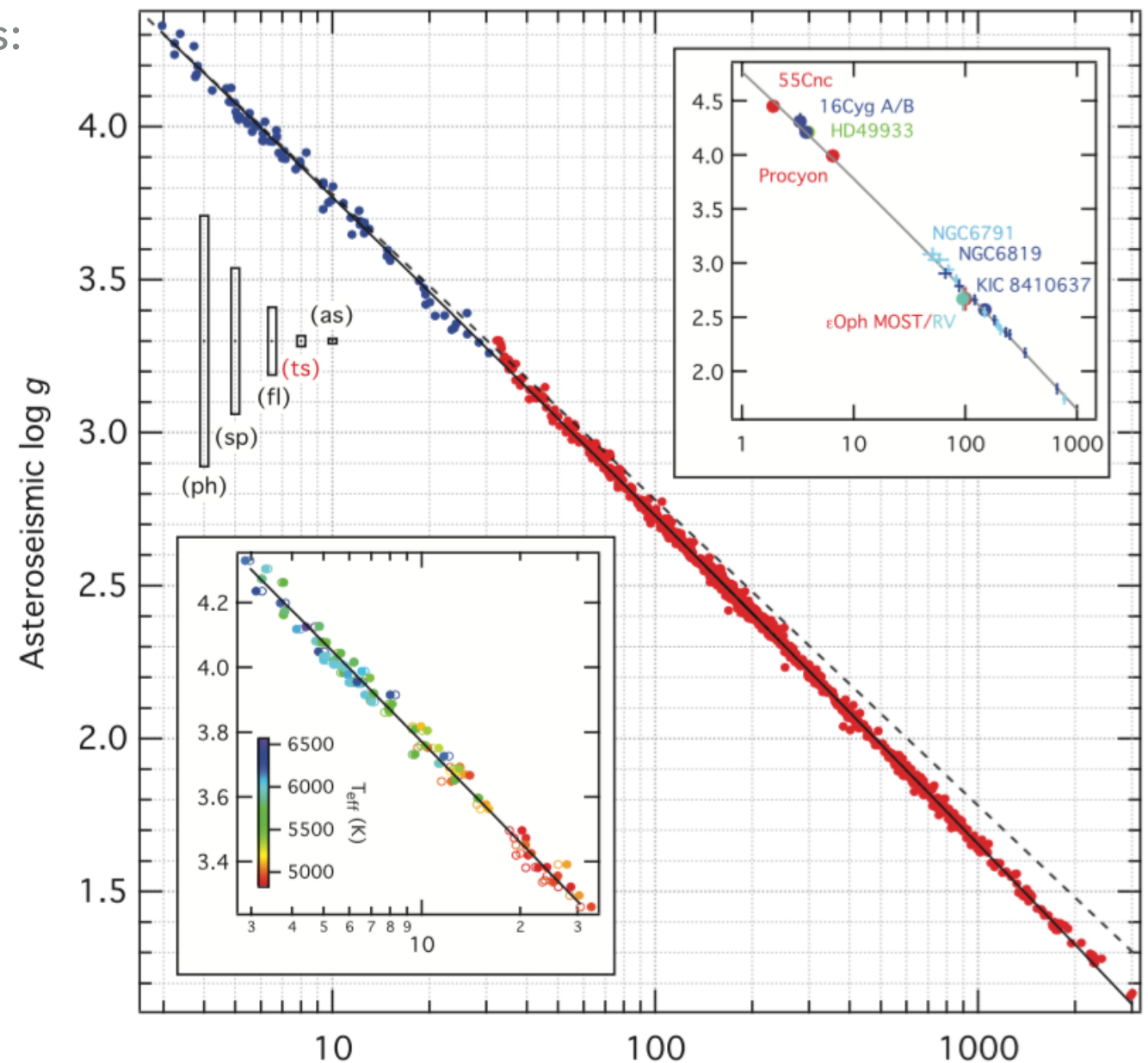


AUTOCORRELATION TIMESCALE

calibration with seismic surface gravity gives:

$$\log g = 4.766 \pm 0.007 - 0.962 \pm 0.007 \log(\tau_{ACF}) - 0.026 \pm 0.002 \log(\tau_{ACF})^2$$

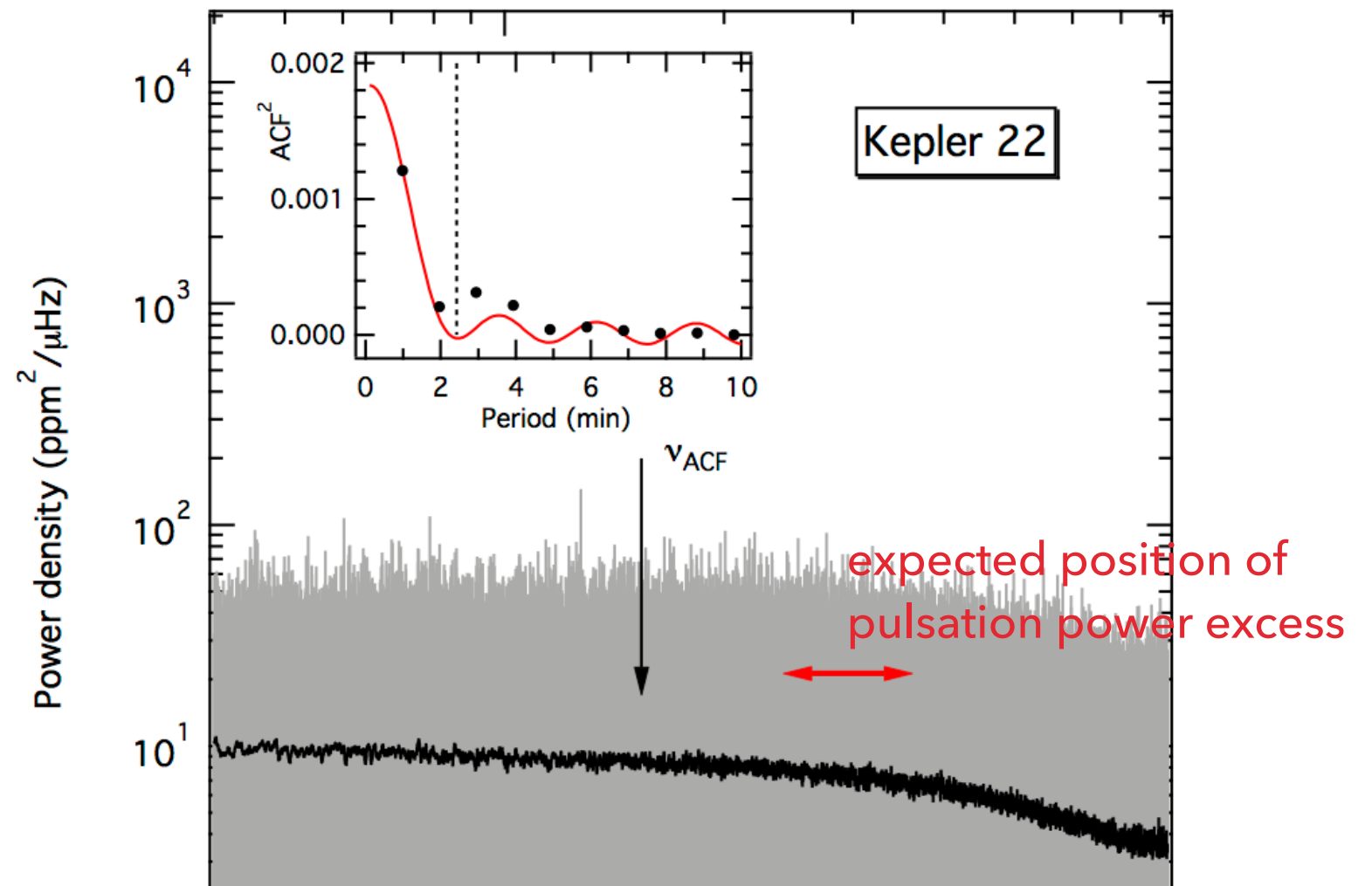
accurate to ± 0.017 (or ~4%)



surface gravity

autocorrelation timescale

WORKS ALSO FOR “NOISY” STARS



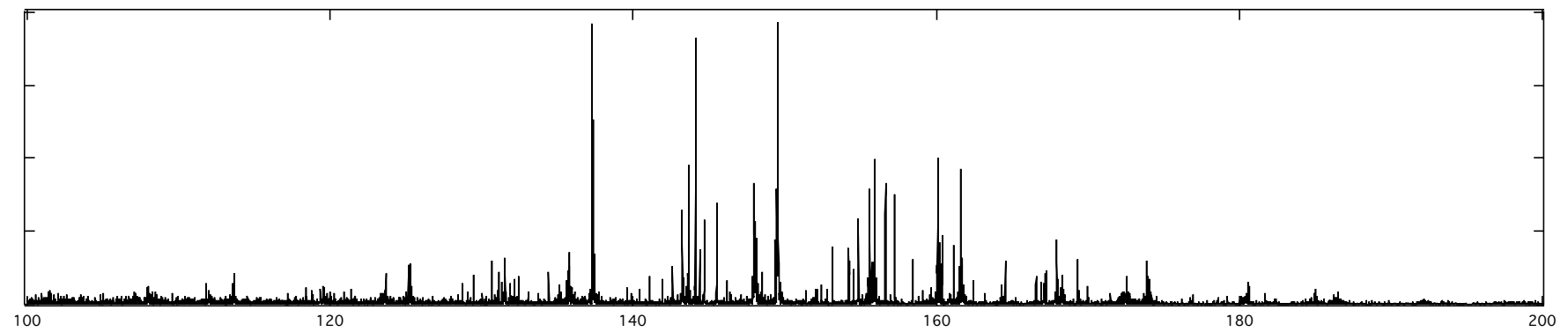
ACF technique: $\log g = 4.39 \pm 0.04$

spectroscopy: $\log g$

large potential for future missions (e.g. TESS)

MODE LIFETIMES ON THE RGB

PROBLEM



large number of modes

due to mixed nature of nonradial modes the total number of modes rapidly exceeds 100

rotationally split modes

rotation splits nonradial modes into multiplets with an a priori unknown structure (single peak/duplet/triplet for $l=1$ modes)

lifetime effects

is a more resolved or not? does a peak belong to a poorly resolve Lorentzian profile or is it a individual mode?

mode identification

unknown spherical degree

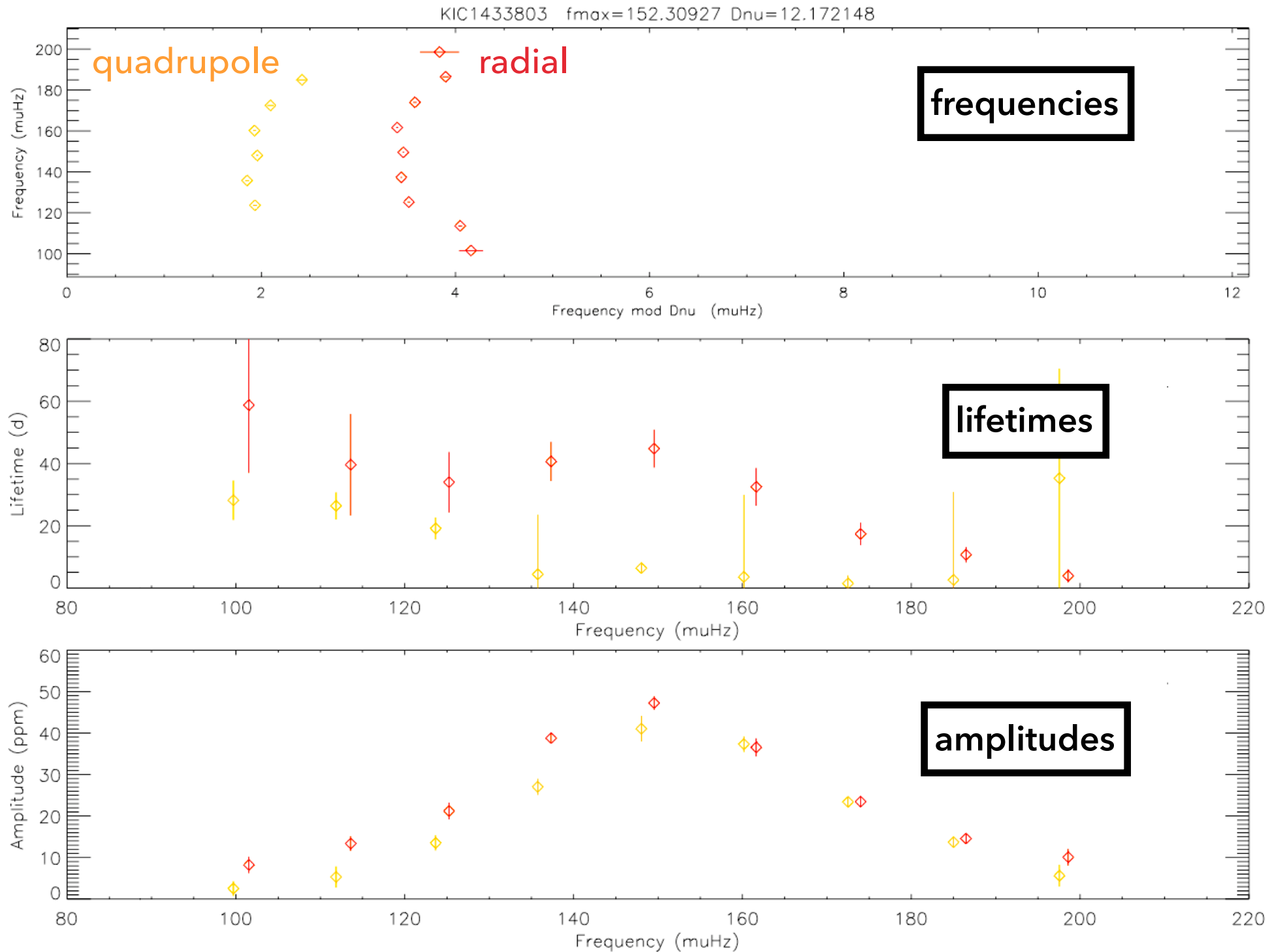
mode significance

is a peak due to noise?

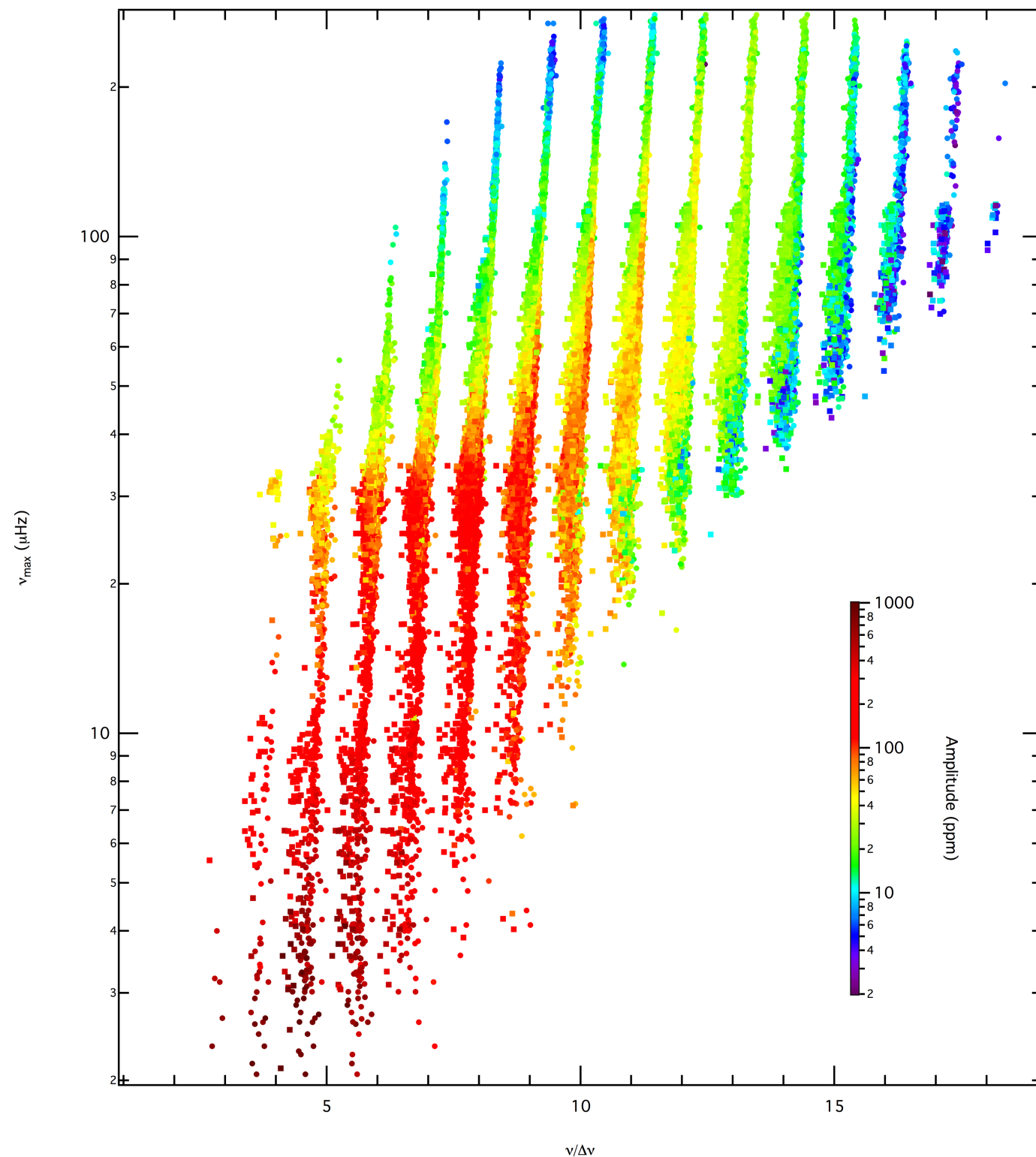
for thousands of star  automatic approach

**I SPARE YOU THE DETAILS
(BUT ITS COMPLICATED)**

L = 0 AND 2 MODES



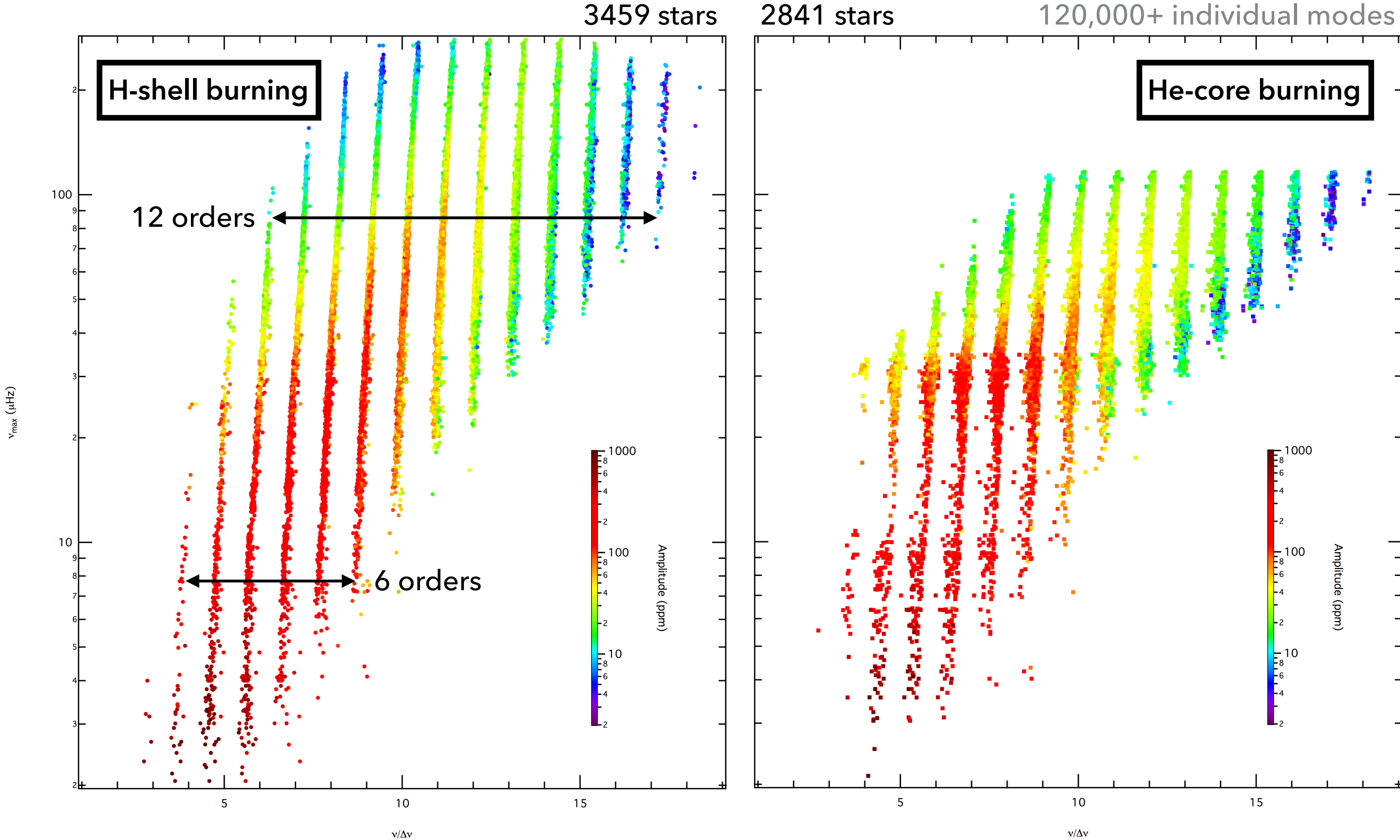
APOKASC SAMPLE



radial modes with
Bayesian evidence > 0.95
of **6300** stars

(~42,000 modes)

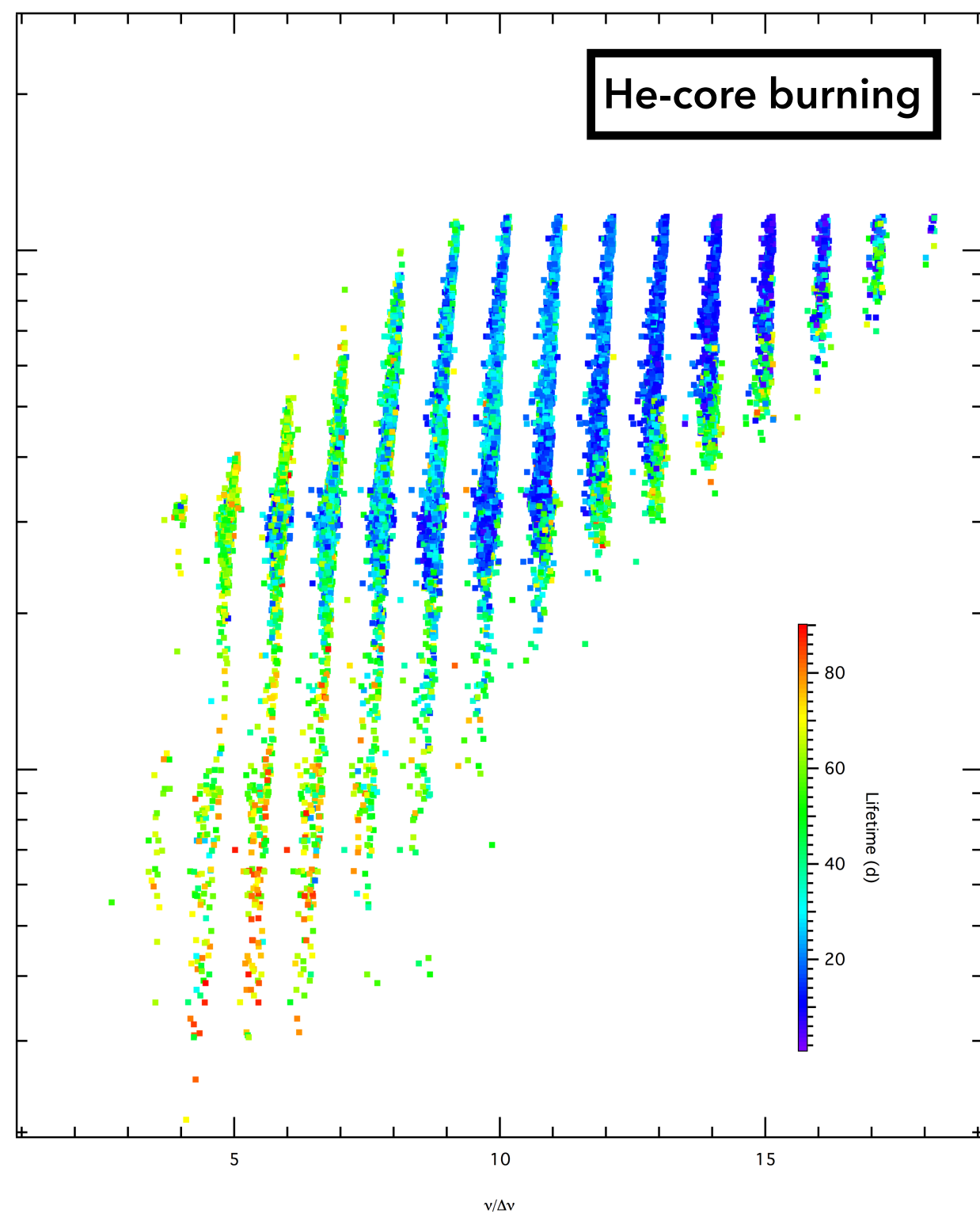
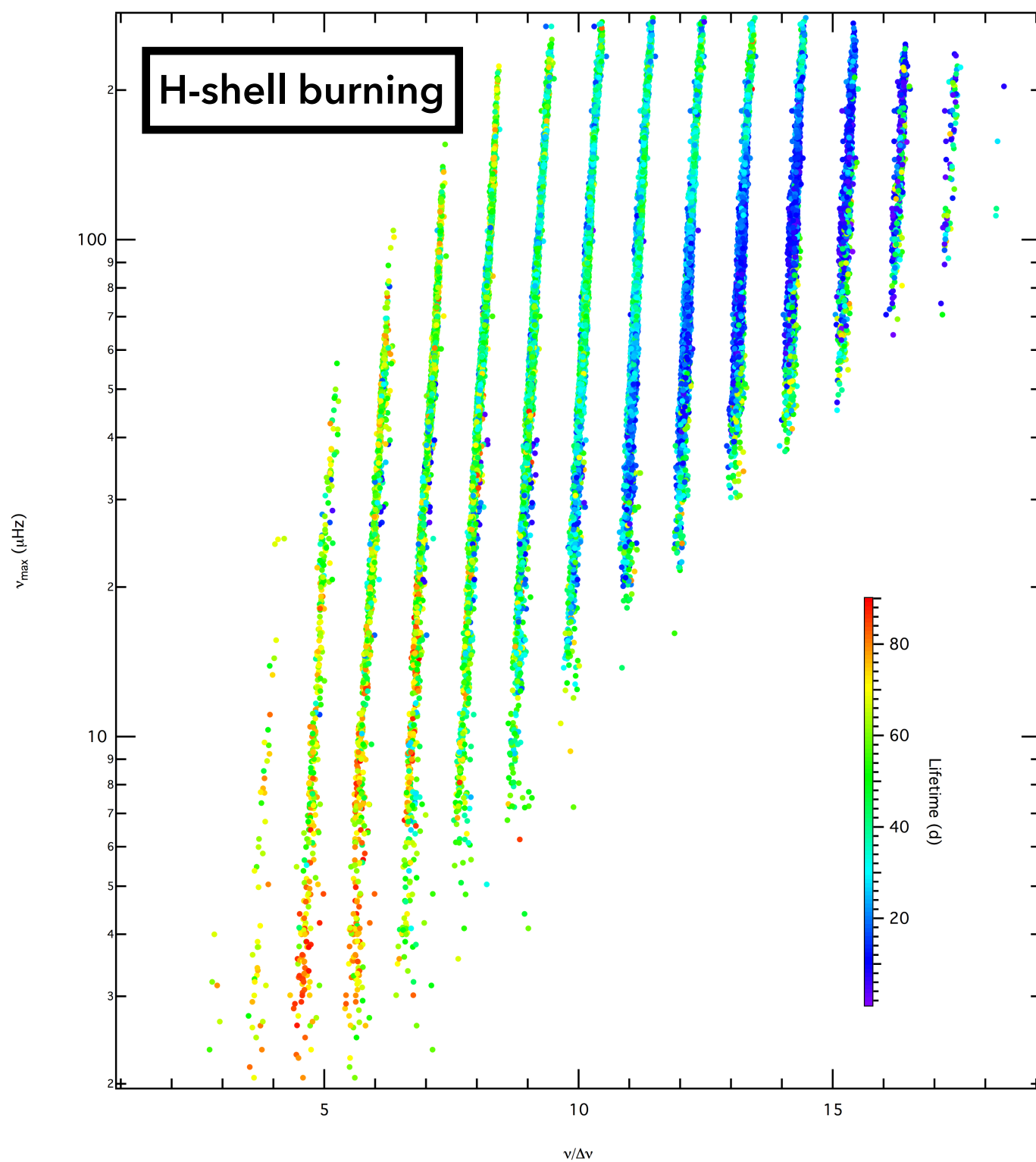
APOKASC SAMPLE



APOKASC SAMPLE

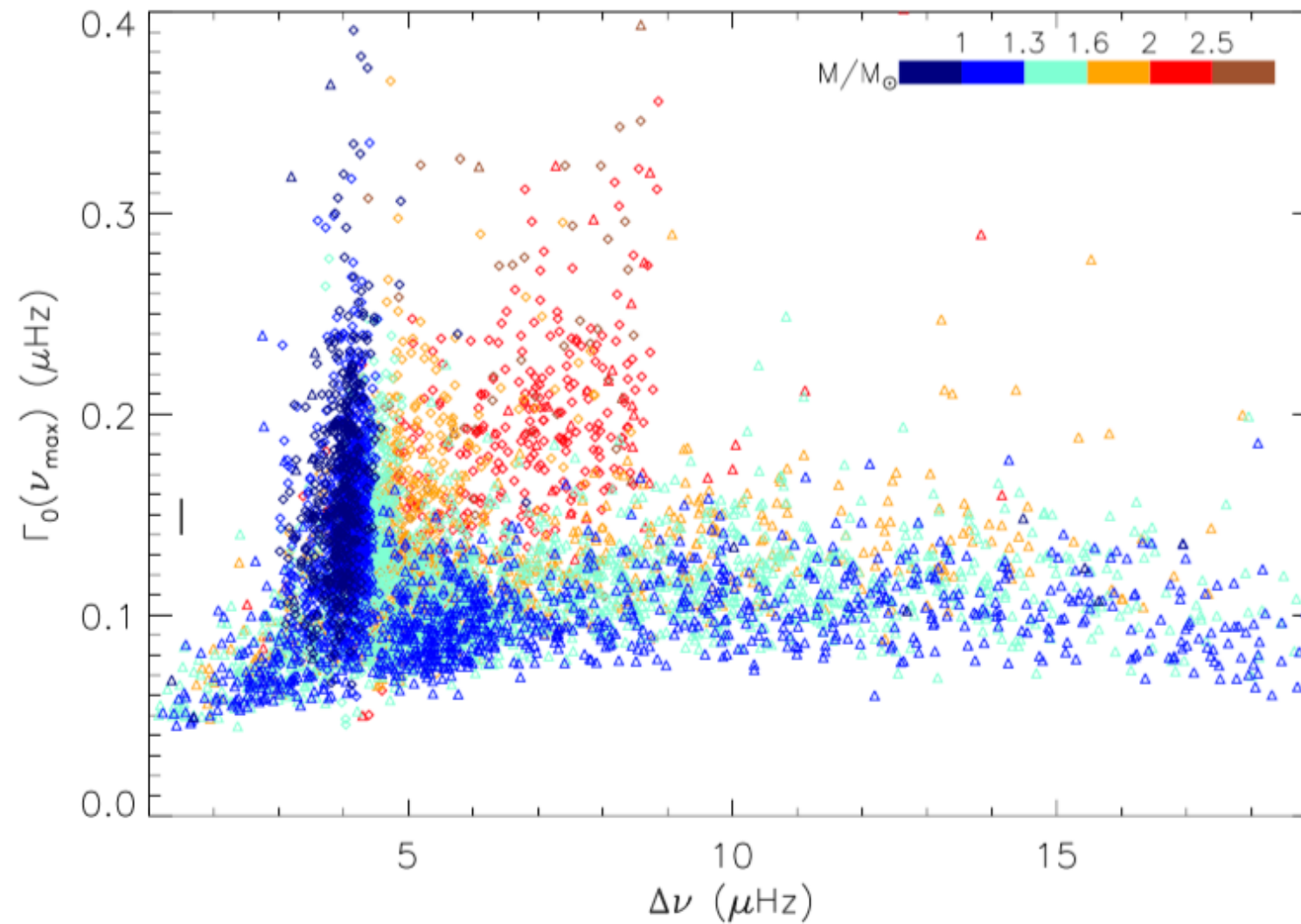
3459 stars

2841 stars

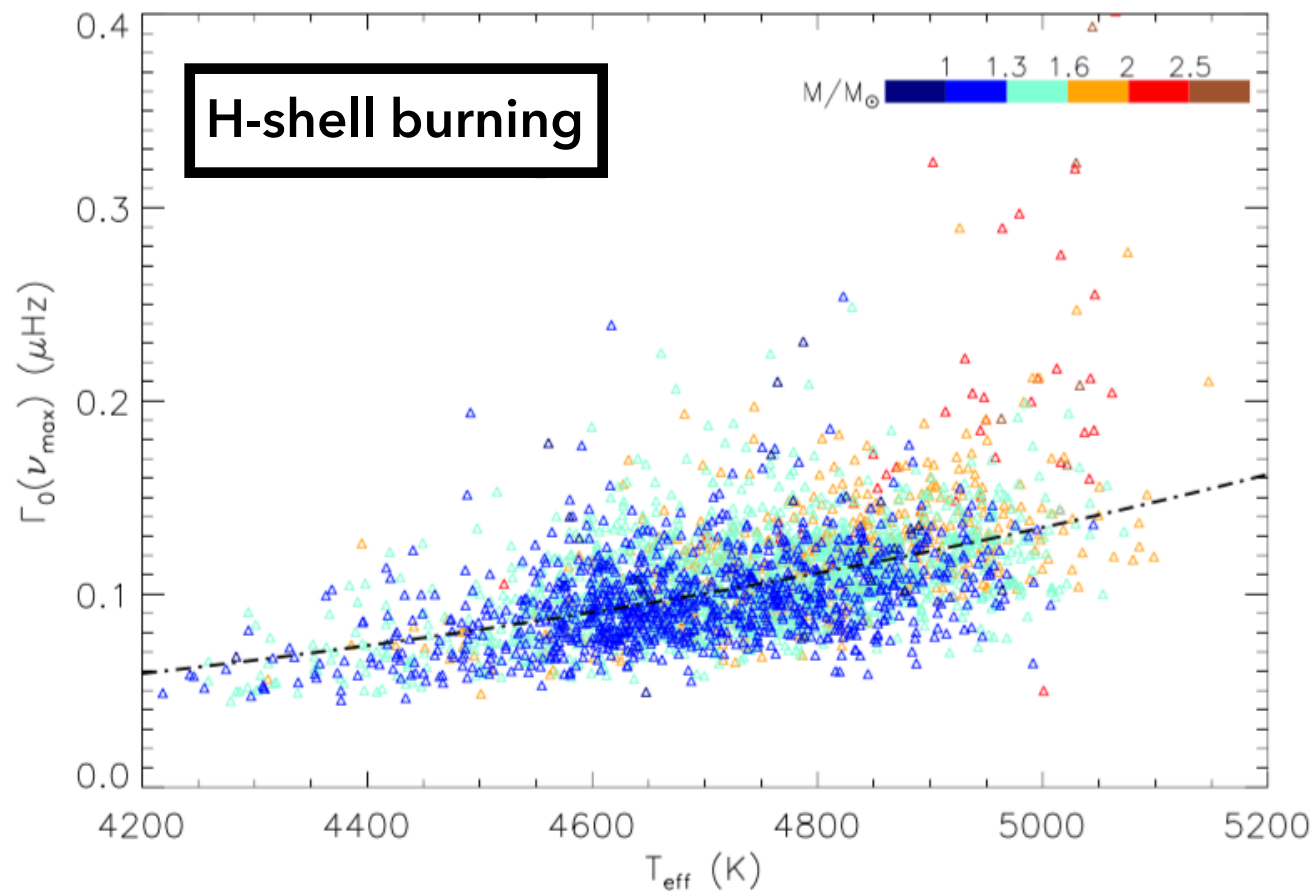


LINE WIDTHS IN THE CENTRE OF THE POWER EXCESS

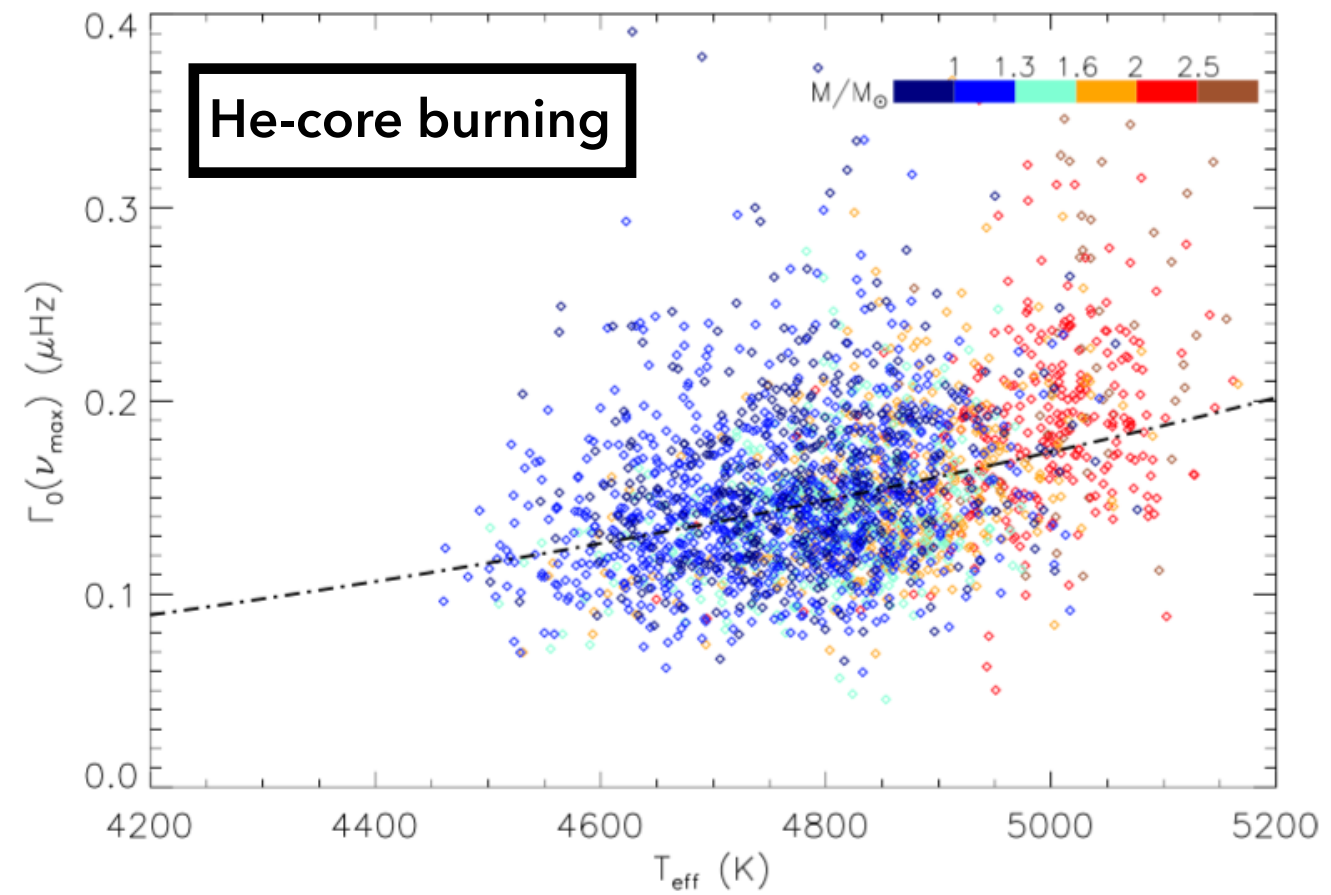
Vrard & Kallinger (in prep)



TEMPERATURE SCALING



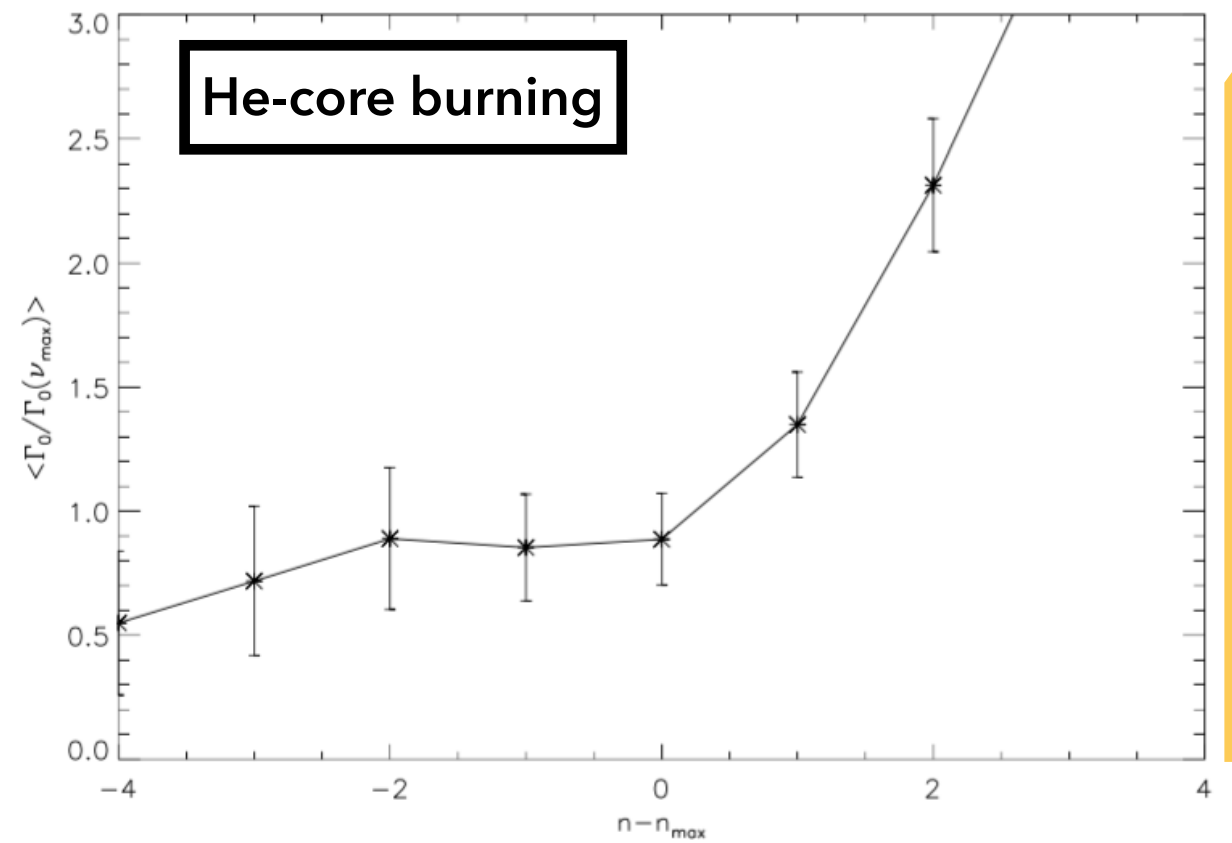
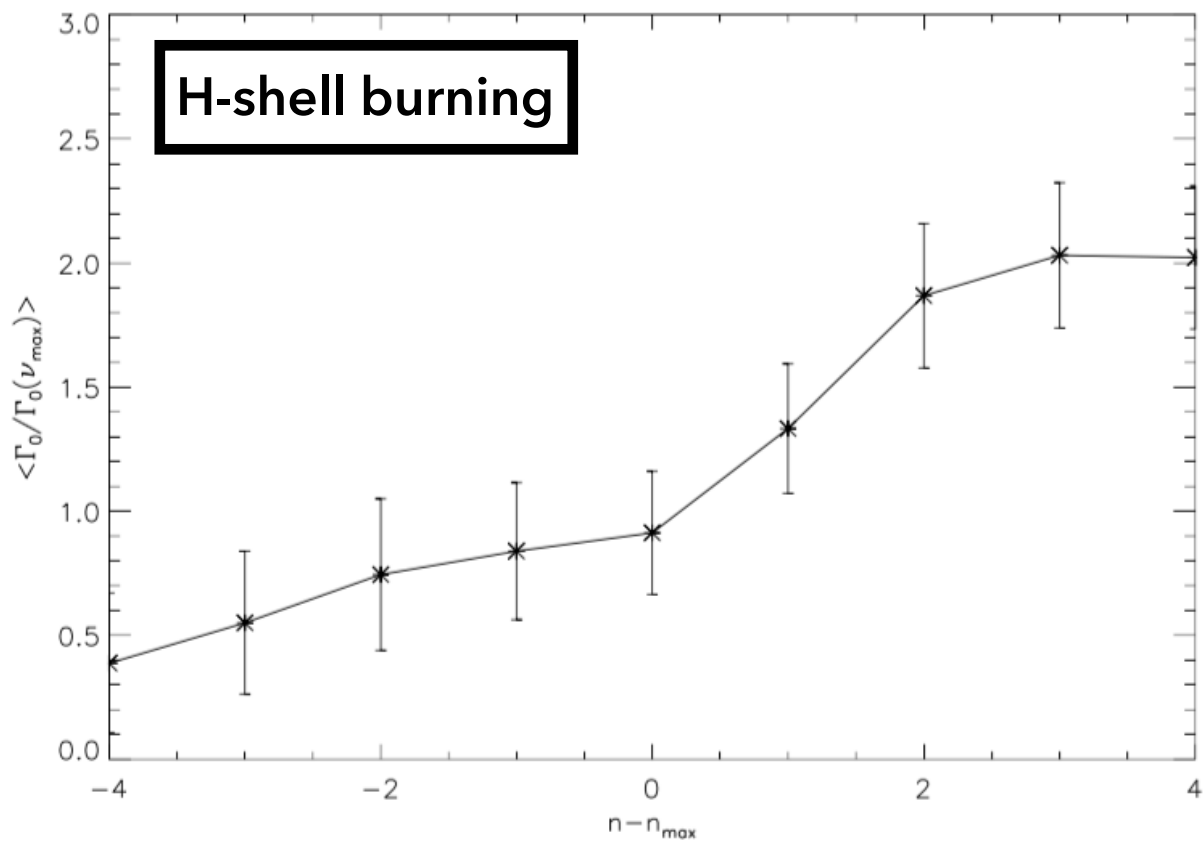
$$\Gamma(\nu_{\max}) \sim T_{\text{eff}}^{4.8}$$



$$\Gamma(\nu_{\max}) \sim T_{\text{eff}}^{3.8}$$

FREQUENCY DEPENDENCE

collapsograms of all stars



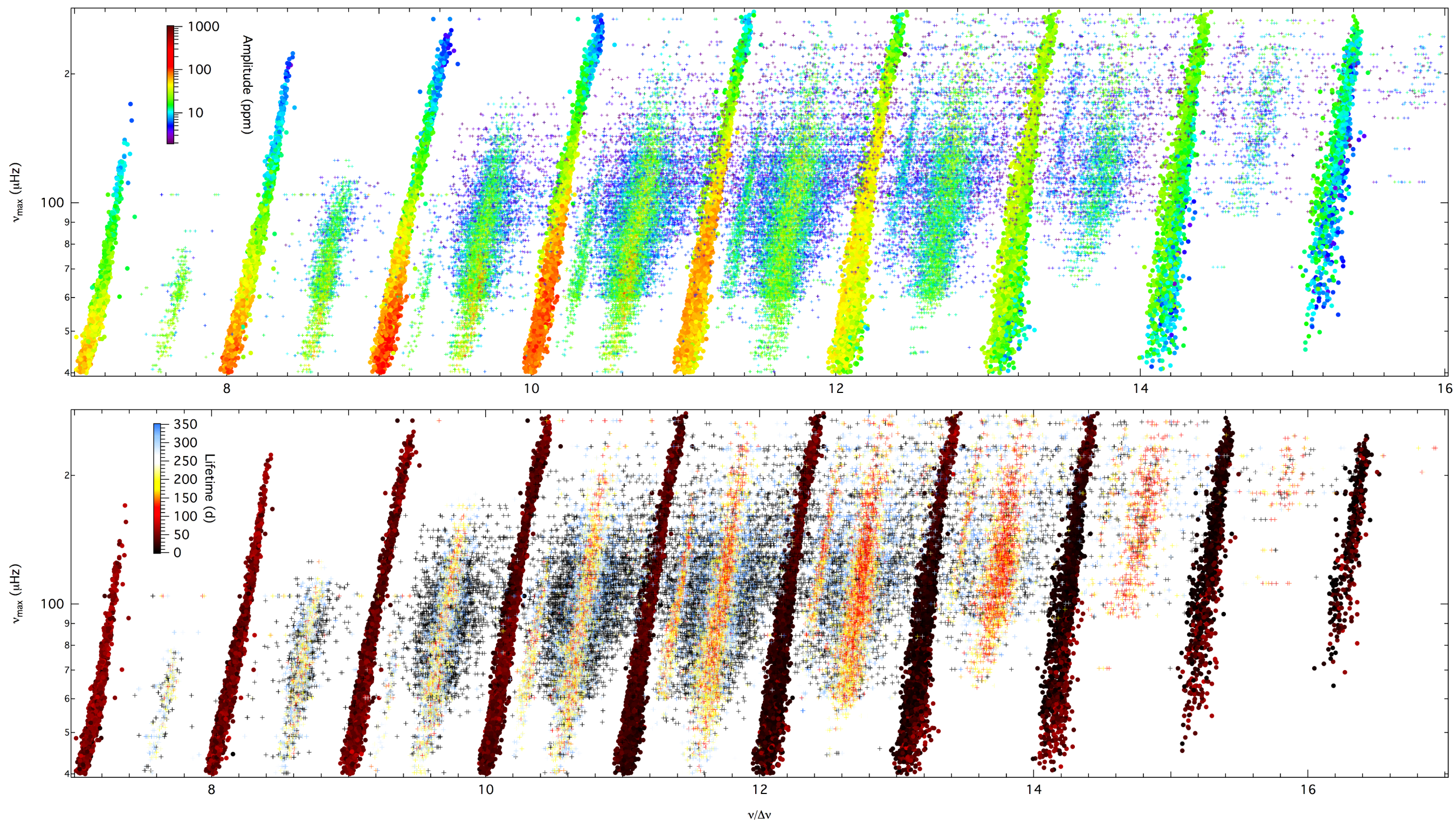
relative line width

relative radial order

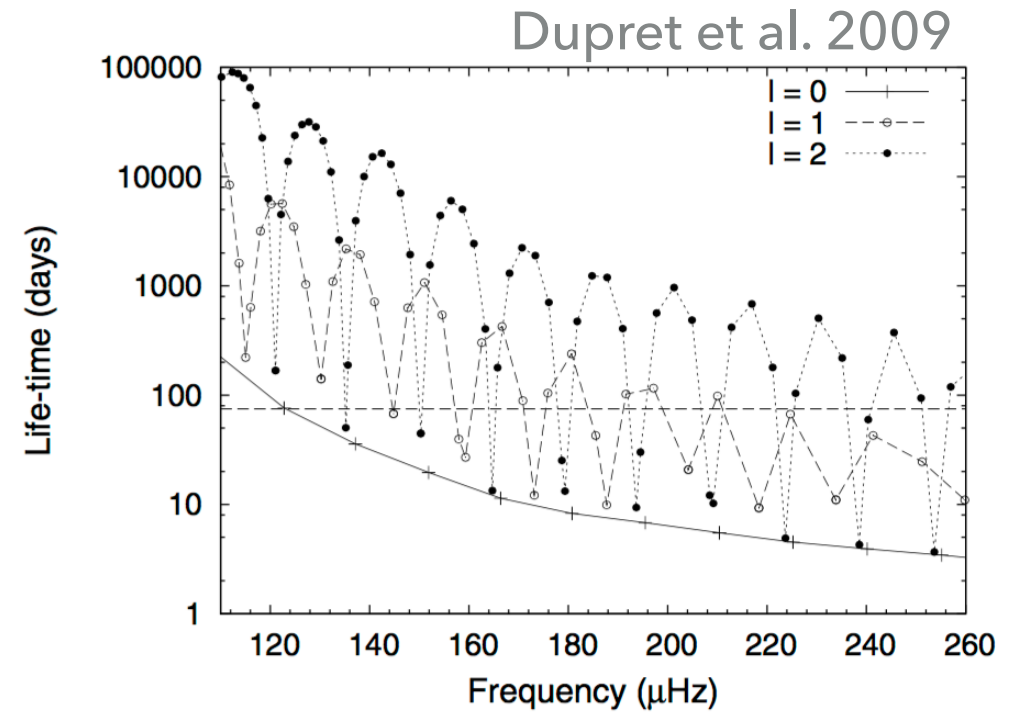
NON-RADIAL MODES

APOKASC SAMPLE

~2800 RGB stars with $\nu_{\max} > 30 \mu\text{Hz}$



THEORETICAL - OBSERVED



60,000+ individual modes

